

An Introduction to the Dual Active Bridge Converter or DAB

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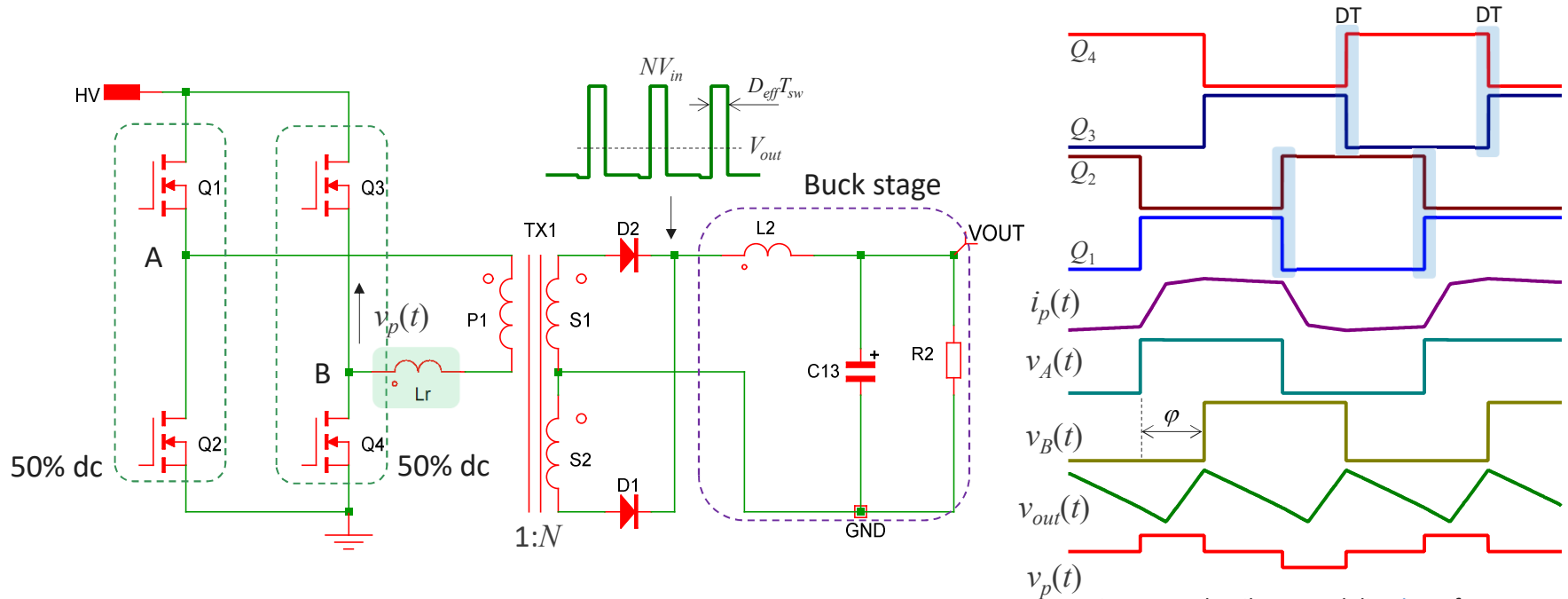
IEEE Senior Member

Agenda

- Phase-Shift Control
- Determining Inductor Currents
- Controlling the Power Flow
- Current Stress in the Converter
- Transformer Operating Point
- Switching Losses
- Small-Signal Response

Phase-Shift Modulation

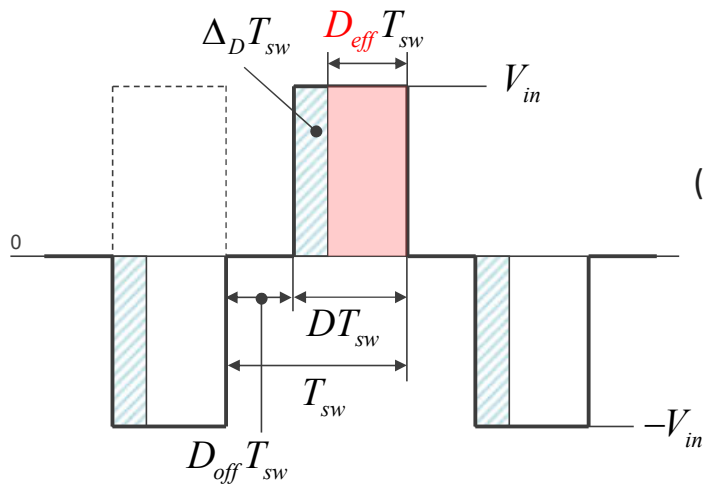
- A classical full-bridge converter is a buck-derived topology
- The dc transfer characteristic depends on the effective duty ratio D_{eff}
- ZVS can be obtained in the primary side but may be a problem in light load



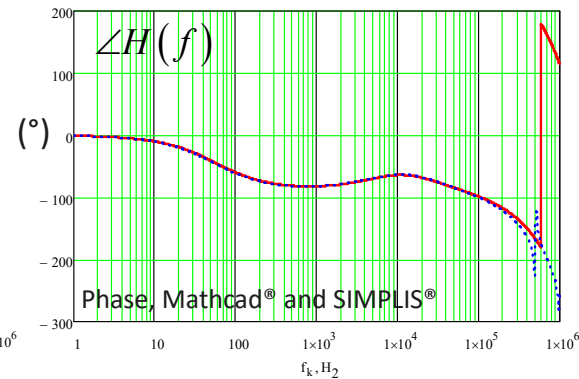
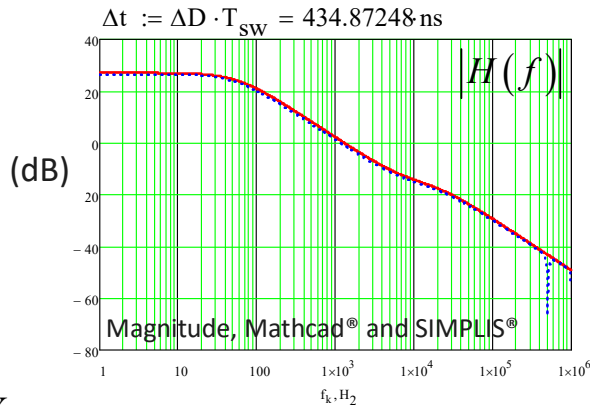
See more details on modeling [here](#) from my webpage

Small-Signal Response of the PSFB

- The control-to-output transfer function of the PSFB shows no resonating peak
- Inherent current feedback effectively damps the system: d_{eff} reduces if I_{out} increases



$$\Delta D = \frac{n \left[2I_{out} - T_{sw} \frac{V_{out}}{L} (1-D) \right]}{\frac{V_{in}}{l_{leak}} T_{sw}}$$

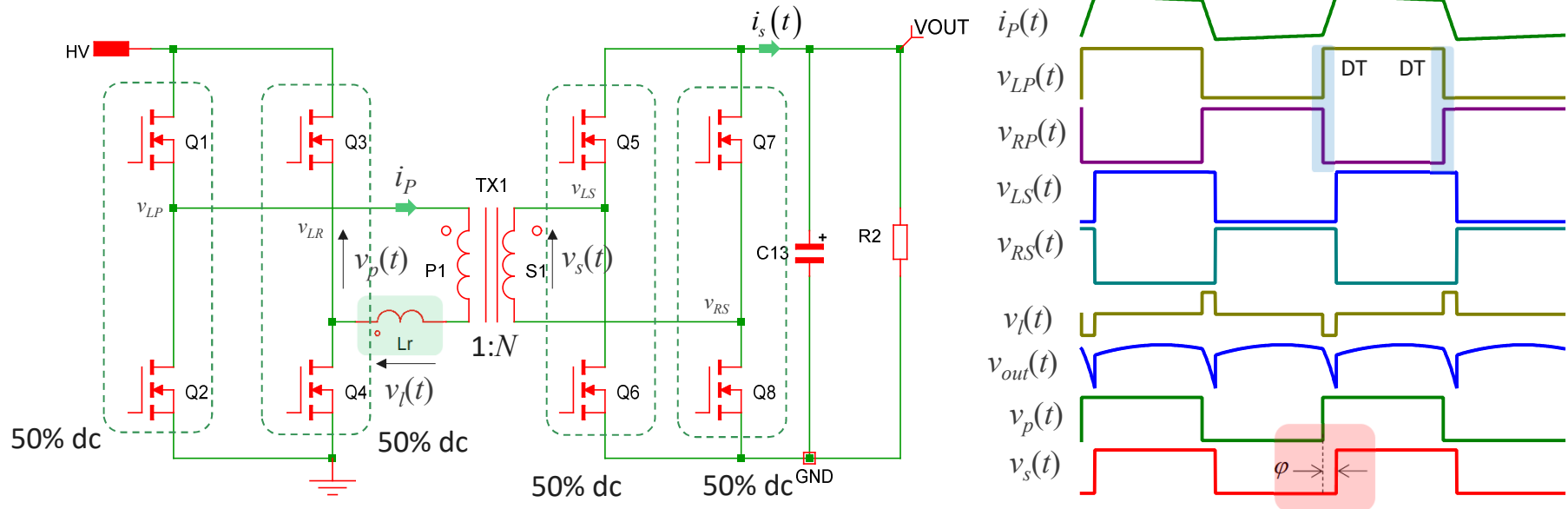


$$H_2(s) := \frac{N_1 \cdot R_L \cdot V_{in}}{R_L + R_d} \cdot \frac{1 + s \cdot r_C \cdot C_1}{1 + s \cdot \left(\frac{L_1 + C_1 \cdot R_L \cdot R_d}{R_L + R_d} \right) + s^2 \cdot \frac{C_1 \cdot L_1 \cdot R_L}{R_L + R_d}} \cdot e^{-s \cdot \Delta t}$$

$$H(s) = H_0 \frac{1 + \frac{s}{\omega_z}}{1 + \frac{s}{\omega_0 Q} + \left(\frac{s}{\omega_0} \right)^2} e^{-s \Delta t} \quad Q = \frac{\sqrt{b_2}}{b_1} \quad \omega_0 = \frac{1}{\sqrt{b_2}}$$

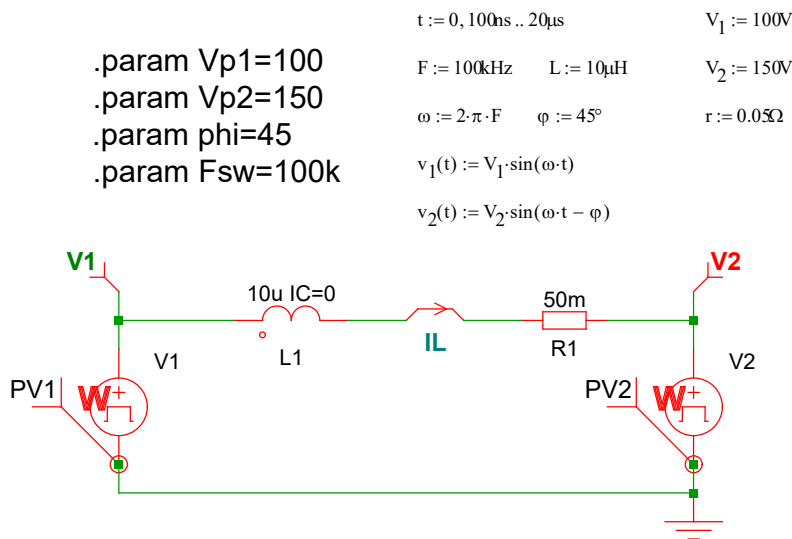
Controlled Rectification

- The dual active bridge or DAB implies a second controlled bridge for rectification
- A single series inductor located in the primary side sizes the power flow
- Power transfer takes place from the leading bridge to the lagging bridge
- ✓ Depending on the angle polarity, power can flow in either direction



Power Transfer between Sinusoidal Sources

- A simplified view to the converter implies two sinusoidal sources and an inductor
- The sources operate at the same frequency and the phase between them is adjusted
- ✓ By changing the phase shift between sources, power flow is adjusted



Instantaneous power

$$p(t) = \frac{V_1 \cdot e^{i \cdot \omega \cdot t} - V_2 \cdot e^{i \cdot (\omega \cdot t + \phi)}}{i \cdot L \cdot \omega} \cdot (V_1 \cdot e^{i \cdot \omega \cdot t})$$

Instantaneous current

$$P = 2 \cdot F_{sw} \cdot \int_0^{2 \cdot F_{sw}} \left(\frac{v_L(t)}{Z_L} \right) \cdot v_1(t) dt$$

Complex power is computed as $P = UI^*$

$$\frac{V_1 \cdot V_2 \cdot \sin(\phi)}{\omega \cdot L} = 1.688 \text{ kW}$$

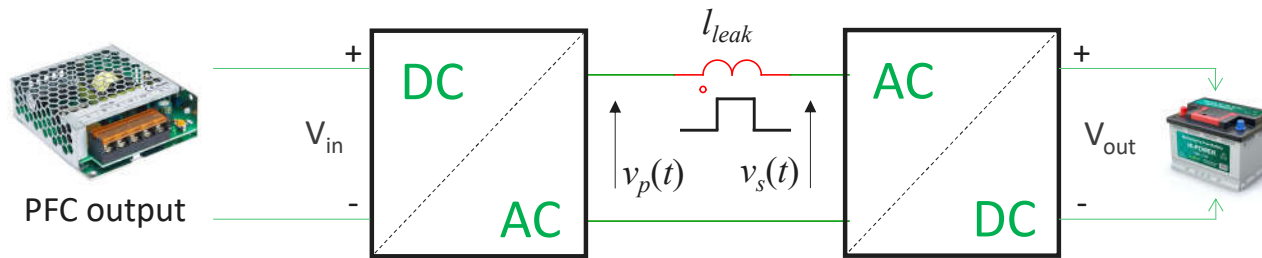
Processed power

$$\text{Re} \left(\frac{V_1 \cdot V_2 \cdot \sin(\phi) - V_1 \cdot V_2 \cdot \cos(\phi) \cdot i + V_1^2 \cdot i}{L \cdot \omega} \right) = 1.688 \text{ kW}$$

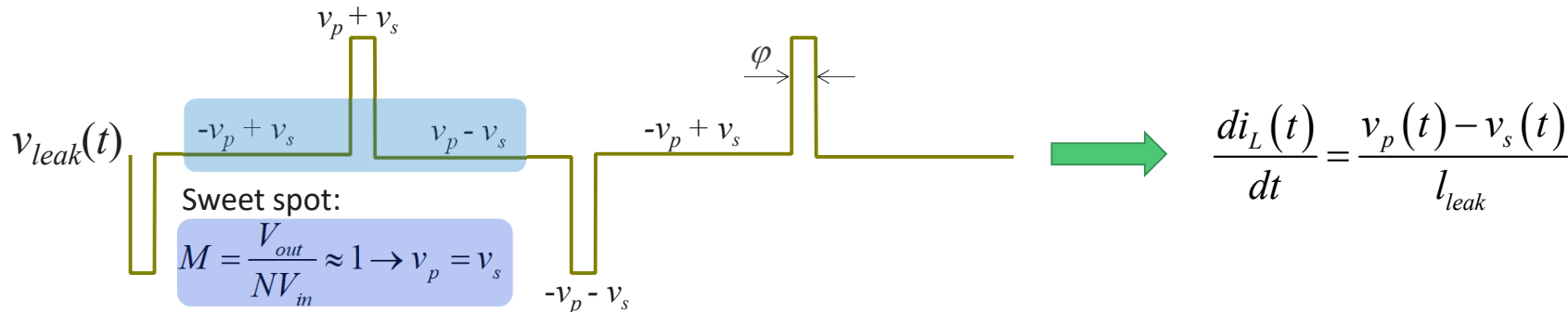
- Changing the sign of the phase reverses the power flow

Power Transfer between Square-Wave Sources

- Power is adjusted by controlling the voltage applied across the leakage inductance
- A transformer brings isolation and provides boost or input voltage reduction



- ✓ Adjusting the phase shift between square waves controls the inductor current

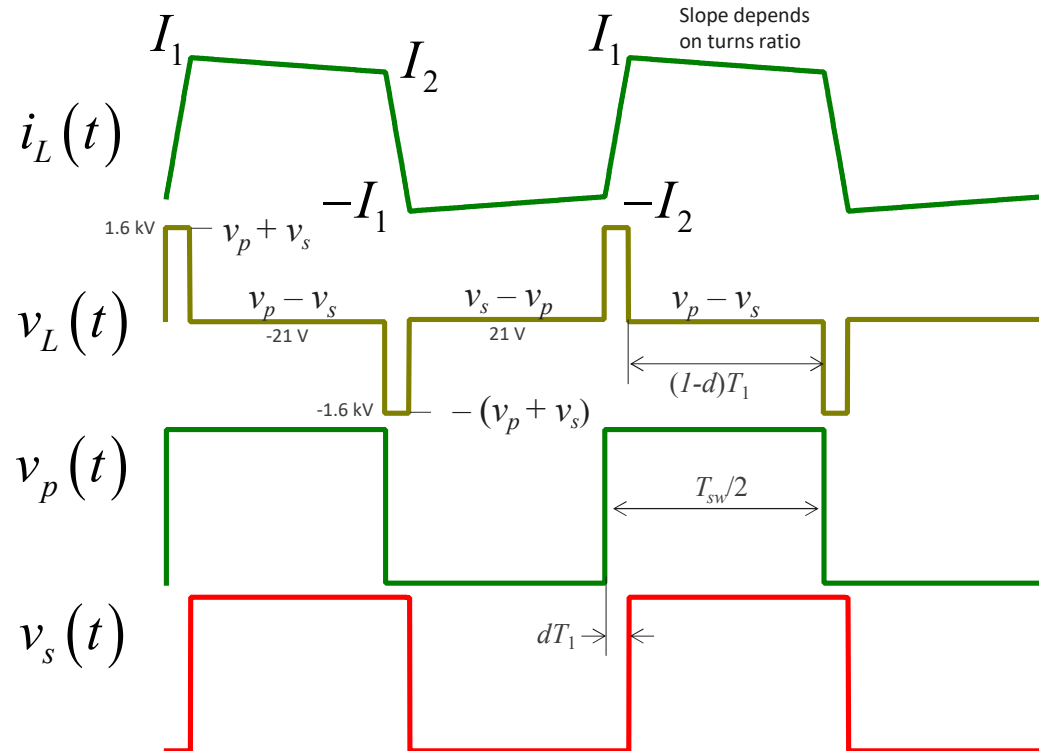


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Determining Inductor Currents

- Power is adjusted by controlling the voltage applied across the leakage inductance
- A transformer brings isolation and scale for boosting or stepping down the voltage



$$I_1 + I_2 = \frac{V_{in} + V_{out} / N}{l_{leak}} dT_1$$

$$I_1 - I_2 = \frac{V_{out} / N - V_{in} (1 - d)}{l_{leak}} T_1$$



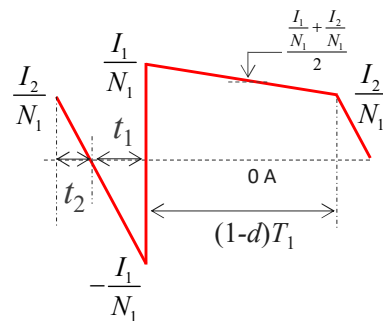
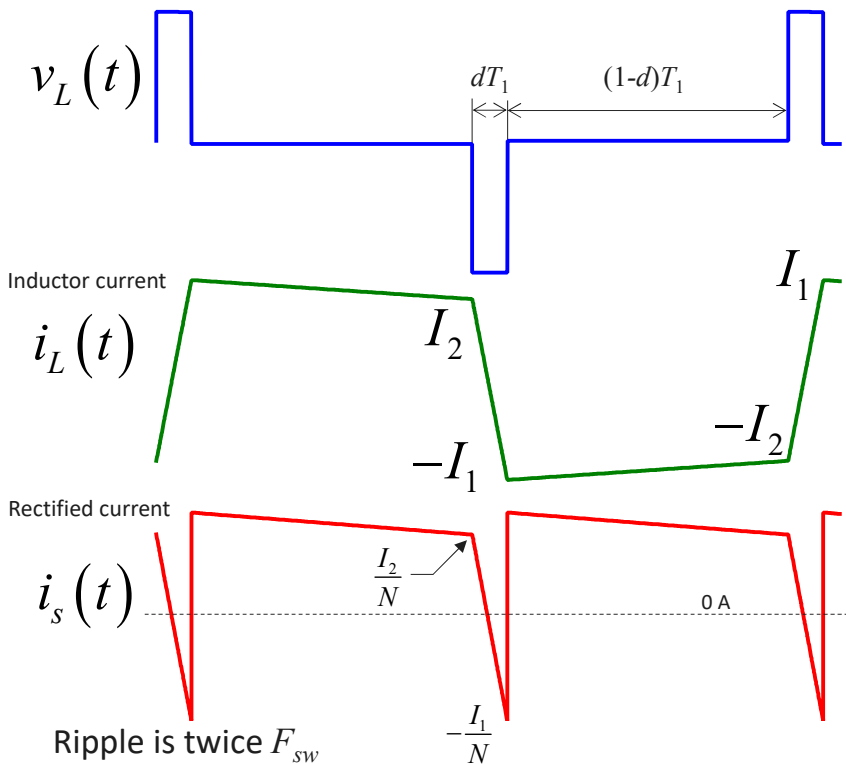
$$I_1 = \frac{T_1 (V_{out} - NV_{in} + 2N \cdot d \cdot V_{in})}{2Nl_{leak}}$$

$$I_2 = \frac{T_1 (2 \cdot d \cdot V_{out} + NV_{in} - V_{out})}{2Nl_{leak}}$$

$$T_1 = 1 / (2F_{sw})$$

Calculating the Output Power

- The primary inductive current is scaled by the turns ratio and flows in the secondary
- Determining its average rectified value leads to the delivered power



$$t_1 = \frac{I_1 N l_{leak}}{V_{out} + N V_{in}}$$

$$t_2 = \frac{I_2 N l_{leak}}{V_{out} + N V_{in}}$$

$$t_1 + t_2 = d T_1$$

$$\langle i_s(t) \rangle_{T_{sw}} = \frac{\left(\frac{I_2 t_2}{N 2} - \frac{I_1 t_1}{N 2} \right) + \frac{I_2 + I_1}{2} (1-d) T_1}{T_1}$$



Insert I_1 and I_2 from previous slide, rearrange

$$P_{out} = I_s V_{out} = \frac{d(1-d) T_{sw} V_{in} V_{out}}{2 N l_{leak}}$$

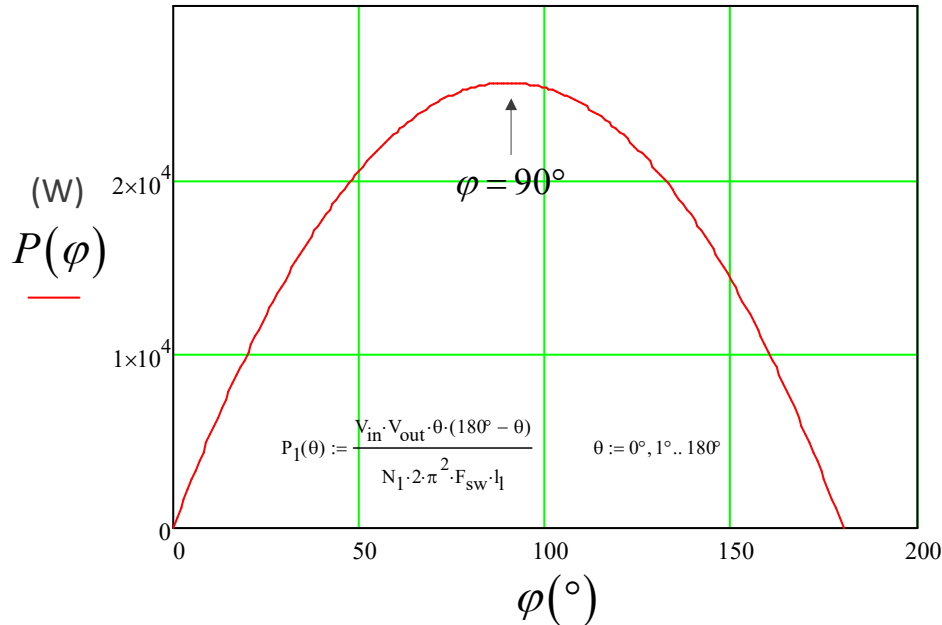
$$T_1 = 1/(2F_{sw})$$

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Controlling the Power Flow

- Varying the duty ratio or the phase-shift between bridges adjusts the power flow
- The transmitted power is maximal when the angle reaches 90° or $\pi/2$



- ✓ The sign of the angle determines the power transfer direction
- ✓ The controlling angle must be bounded to keep the same control law slope:

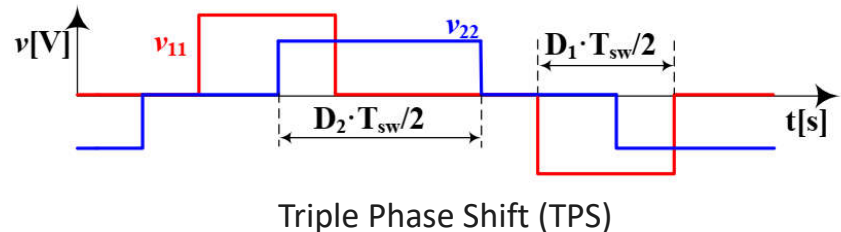
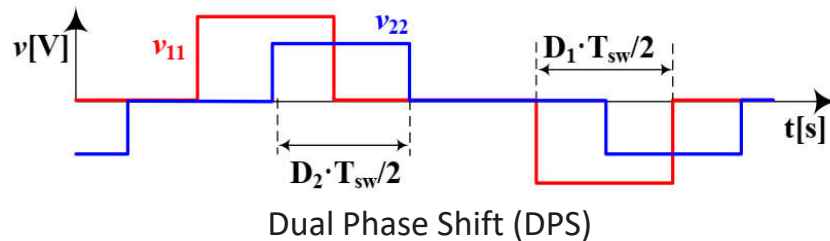
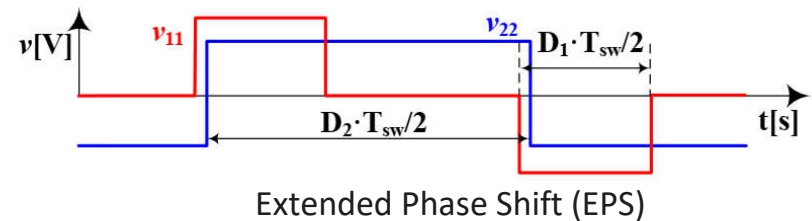
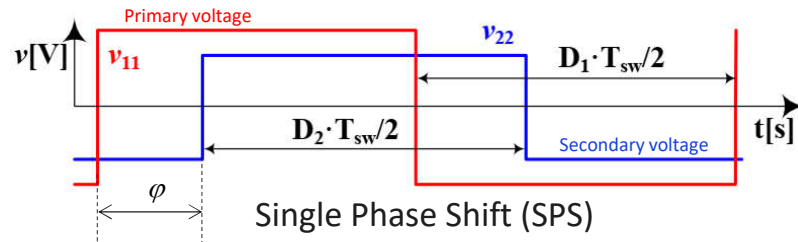


$$D_1 \in [0; 50\%] \quad D_2 \in [0; 50\%] \quad \varphi \in \left[-\frac{\pi}{2}; \frac{\pi}{2} \right]$$

$$P_{out} = \frac{V_{in} V_{out} \cdot \varphi \cdot (180^\circ - \varphi)}{2\pi^2 N F_{sw} l_{leak}}$$

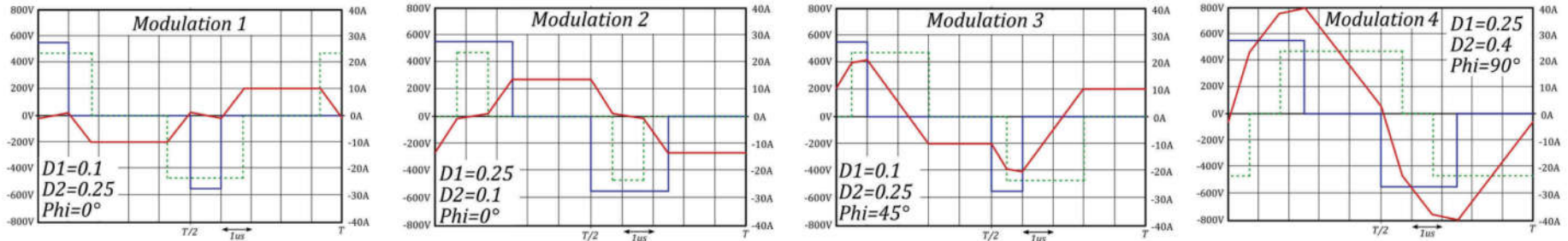
Different Types of Modulations

- Different strategies exist to modulate the power flow with different control variables
- ✓ Single phase shift implies 50% duty ratio for both bridges and phase modulation
- ✓ Dual phase shift with variable *equal* duty ratios and phase shift adjustment
- ✓ Triple phase shift where both duty ratios are modulated with phase shift control

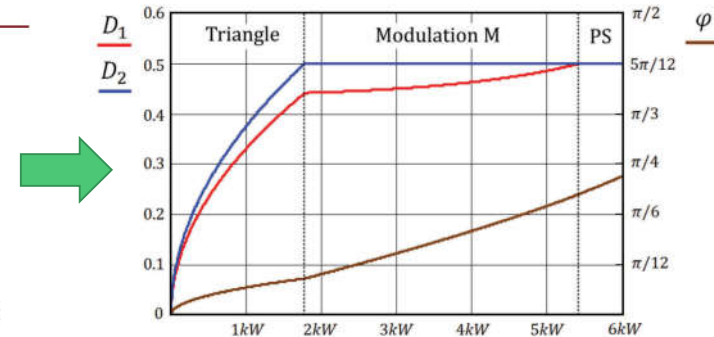


Minimizing Rms Currents

- Various modulation strategies can be explored to minimize the circulating rms currents
- The aim is to reduce conduction losses and reactive power while ensuring ZVS



Mod. name	Advantage	Drawbacks	Others characteristics
Phase-shift	Easy control	Maximal power	Loss of ZVS
Triangle	ZVS	Limited power when $V1$ is closed to $n.V2$	1 degree of freedom
Trapezium	ZVS	Reduced power compared to phase-shift	2 degrees of freedom
1	Reduced RMS current compared to phase-shift	Loss of ZVS depending on parameters values	Special case of Mod.1 and 2
2		Limited power	2 degrees of freedom
3			2 degrees of freedom
4			2 degrees of freedom
M	Power close to maximum	Maximal power	2 degrees of freedom
	ZVS	Complex control	Special case of Mod.4 when $D_2 = 0.5$

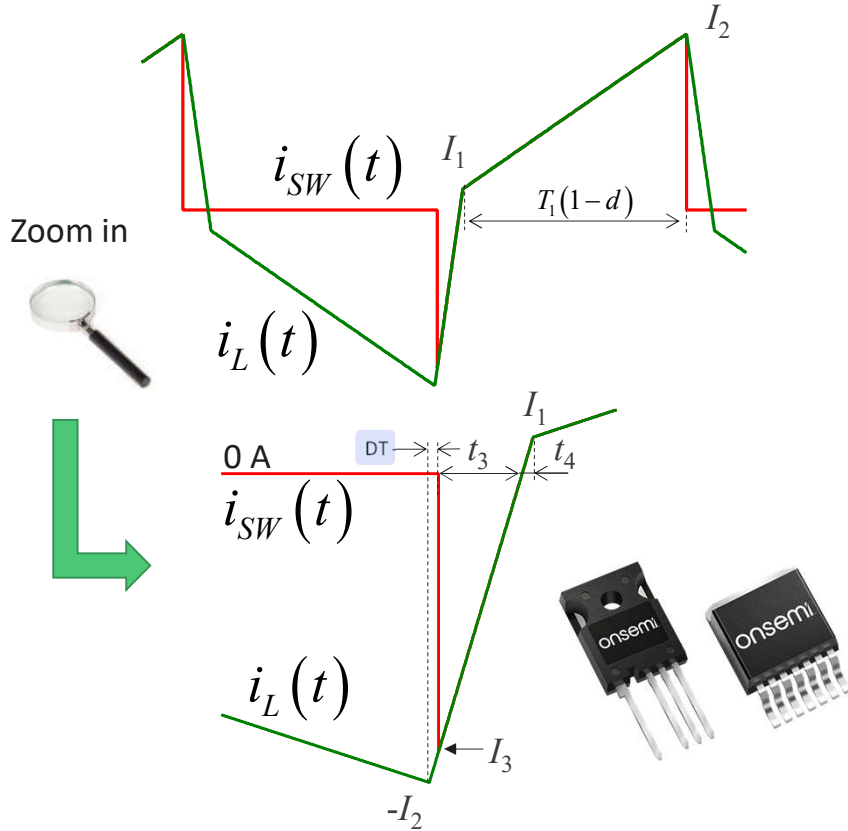


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Rms Current in Primary Switches

- The deadtime plays a role in the circulating current and must be accounted for



- Determine the switch current I_3 after deadtime:

$$I_3 = - \left(I_2 - \frac{V_{in} + \frac{V_{out}}{N}}{I_{leak}} \cdot DT \right) \rightarrow t_3 = \frac{NI_3 I_{leak}}{V_{out} + NV_{in}}$$

- Determine the time from 0 A to I_1 : $t_4 = \frac{NI_1 I_{leak}}{V_{out} + NV_{in}}$

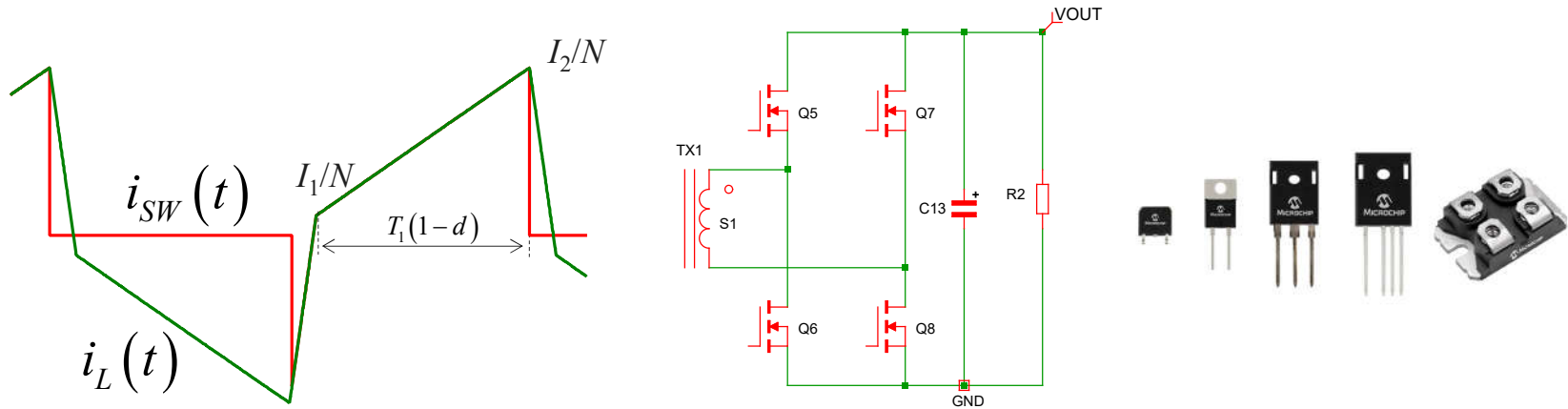
- Sanity check to verify $dT_1 = DT + t_3 + t_4$

- Conduction time $t_5 = T_1(1-d)$

$$I_{SW,rms} = \sqrt{\frac{1}{3T_{sw}}(I_3^2 t_3 + I_1^2 t_4) + \frac{1}{3}(I_1^2 + I_2^2 + I_1 I_2) \frac{t_5}{T_{sw}}}$$

Rms Current in the Secondary Switches

- The secondary-side bridge operates as a synchronous rectifier
- It is important to size the amount of rms current which circulates in these switches



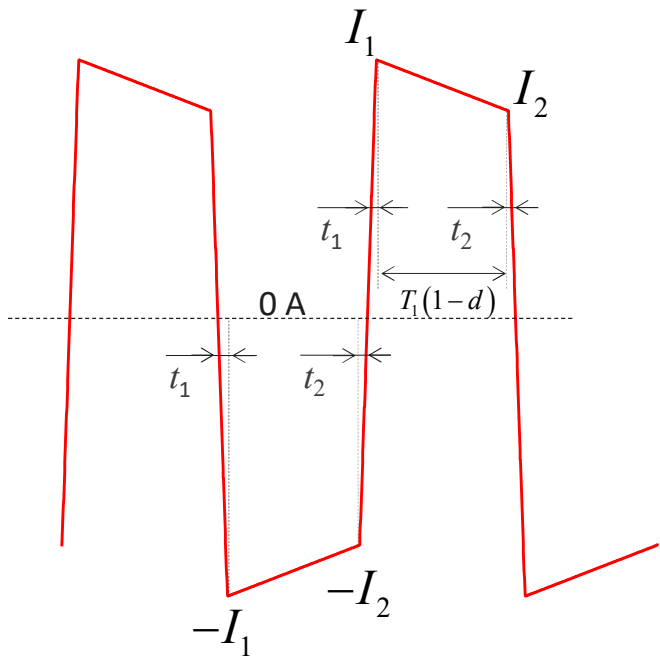
- The secondary-side currents are those of the primary switches scaled by the turns ratio

➔

$$I_{SW,rms} = \sqrt{\frac{1}{3T_{sw}} \left[\left(\frac{I_3}{N} \right)^2 t_3 + \left(\frac{I_1}{N} \right)^2 t_4 \right] + \frac{1}{3} \left[\left(\frac{I_1}{N} \right)^2 + \left(\frac{I_2}{N} \right)^2 + \frac{I_1 I_2}{N^2} \right] \frac{t_5}{T_{sw}}}$$

Rms Current in the Transformer

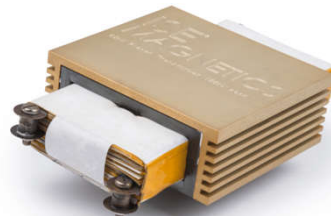
- The transformer and the primary-side inductor see the entire primary current
- It is important to size this rms current as it affects copper losses



$$I_{L,rms} = \sqrt{\frac{1}{3T_1} (I_1^2 t_1 + I_2^2 t_2) + \frac{1}{3} (I_1^2 + I_2^2 + I_1 I_2) (1-d)}$$

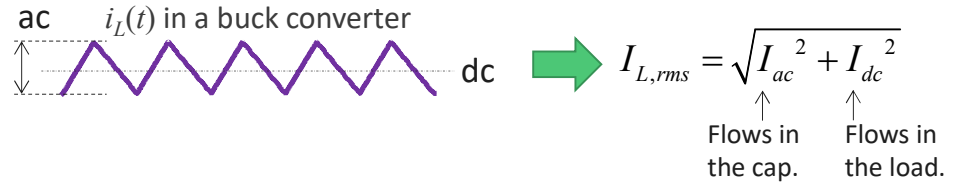
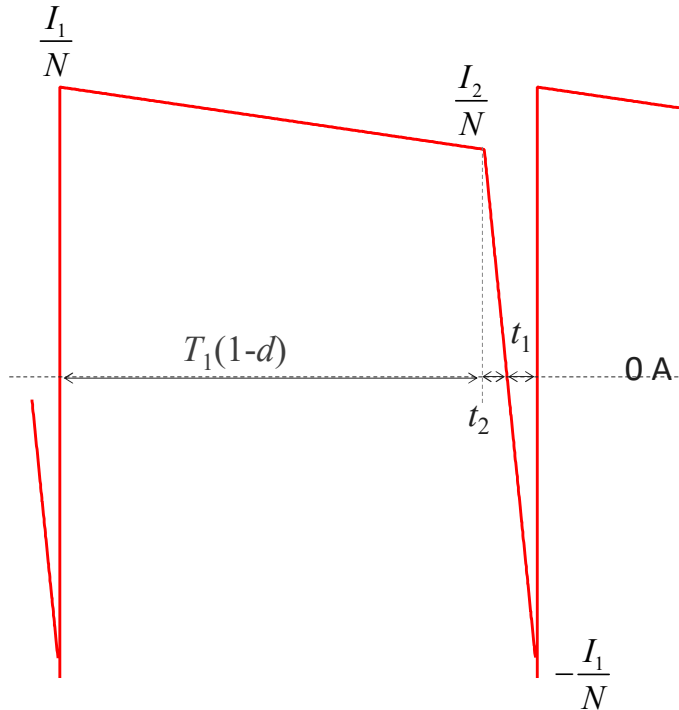
$$I_{L,rms} = \sqrt{\frac{I_1^2}{3} + \frac{I_2^2}{3} + I_1 I_2 \frac{1 - 2\frac{\phi}{180^\circ}}{3}}$$

From TI application note



Rms Current in the Output Capacitor

- It is important to determine the rms current flowing in the output capacitor
- ✓ Operating life-time of the capacitor depends on the correct type selection



$$\langle i_s(t) \rangle_{T_{sw}} = \frac{\left(\frac{I_2 t_2}{N 2} - \frac{I_1 t_1}{N 2} \right) + \frac{I_2 + I_1}{2} (1-d) T_1}{T_1} \quad \text{Dc current}$$

Capacitor rms current

$$I_{s,rms} = \sqrt{\frac{1}{3T_1} \left[\left(\frac{I_1}{N} \right)^2 t_2 + \left(\frac{I_2}{N} \right)^2 t_1 \right] + \frac{1}{3} \left[\left(\frac{I_1}{N} \right)^2 + \left(\frac{I_2}{N} \right)^2 + \frac{I_1 I_2}{N^2} \right] (1-d)}$$

Checking Computed and Simulated Data - 1

- SIMPLIS can deliver the operating point in a few seconds
- It is important to check computed and simulated data before validating calculated values

1st design:

$$V_{in} = 600 \text{ V}$$

$$V_{out} = 500 \text{ V}$$

$$l_{leak} = 32 \text{ } \mu\text{H}$$

$$\text{Turns ratio } N = 625\text{m}$$

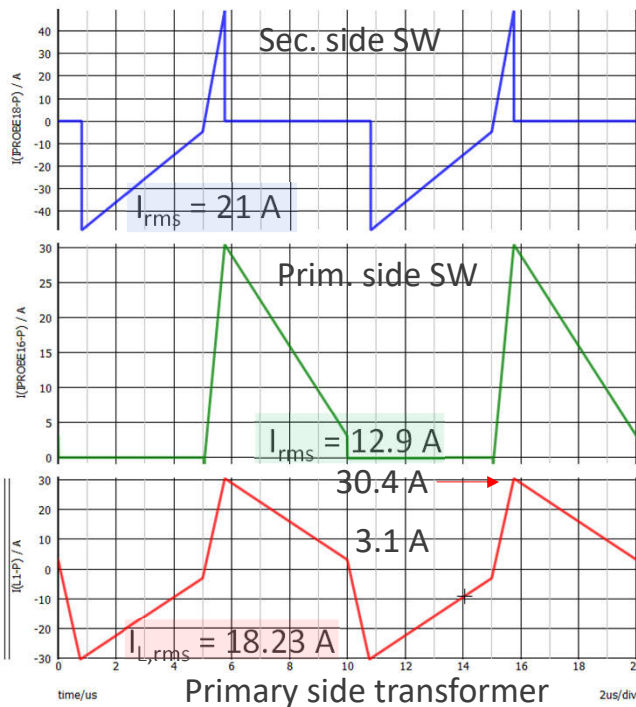
Mathcad®



$$I_1 := \frac{T_1 \cdot (V_{out} - N_1 \cdot V_{in} + 2 \cdot N_1 \cdot V_{in} \cdot d)}{2 \cdot N_1 \cdot l_l} = 30.275\text{A}$$

$$I_2 := \frac{T_1 \cdot (N_1 \cdot V_{in} - V_{out} + 2 \cdot V_{out} \cdot d)}{2 \cdot N_1 \cdot l_l} = 3.402\text{A}$$

$$P_{out} := \frac{(1 - d) \cdot d \cdot T_{sw} \cdot V_{in} \cdot V_{out}}{2 \cdot l_l \cdot N_1} = 9.79\text{ kW}$$



Inductor rms current

$$I_L := \sqrt{\frac{1}{3} \cdot I_2^2 \cdot \frac{t_2}{T_1} + \frac{1}{3} \cdot I_1^2 \cdot \frac{t_1}{T_1} + \frac{1}{3} \cdot [(I_1^2 + I_2^2 + I_1 \cdot I_2) \cdot (1 - d)]} = 18.253\text{A}$$

Sec. switches rms current

$$I_{SW} := \sqrt{\frac{1}{3} \cdot \left(\frac{I_3}{N_1}\right)^2 \cdot \frac{t_3}{T_{sw}} + \frac{1}{3} \cdot \left(\frac{I_1}{N_1}\right)^2 \cdot \frac{t_4}{T_{sw}} + \frac{1}{3} \cdot \left[\left(\frac{I_1}{N_1}\right)^2 + \left(\frac{I_2}{N_1}\right)^2 + \frac{I_1 \cdot I_2}{N_1^2}\right] \cdot \frac{t_5}{T_{sw}}} = 20.649\text{A}$$

Prim. switches rms current

$$I_{SW} := \sqrt{\frac{1}{3} \cdot I_3^2 \cdot \frac{t_3}{T_{sw}} + \frac{1}{3} \cdot I_1^2 \cdot \frac{t_4}{T_{sw}} + \frac{1}{3} \cdot (I_1^2 + I_2^2 + I_1 \cdot I_2) \cdot \frac{t_5}{T_{sw}}} = 12.906\text{A}$$

Output capacitor rms current

$$I_C := \sqrt{I_{outR}^2 - I_{out}^2} = 21.74\text{A} \quad 22 \text{ A rms}$$



Check operating temperature in worst case



Checking Computed and Simulated Data - 2

- In this second operating point, the output voltage is down to 308 V
- ✓ The duty ratio is reduced to 8.6% for that purpose

2nd design:

$$V_{in} = 600 \text{ V}$$

$$V_{out} = 308 \text{ V}$$

$$l_{leak} = 32 \text{ } \mu\text{H}$$

$$\text{Turns ratio } N = 625m$$

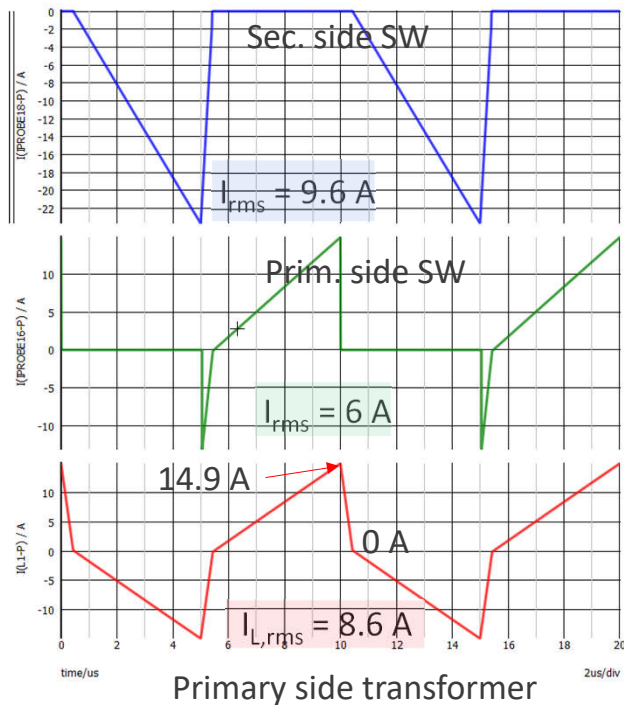
Mathcad®



$$I_1 := \frac{T_1 \cdot (V_{out} - N_1 \cdot V_{in} + 2 \cdot N_1 \cdot V_{in} \cdot d)}{2 \cdot N_1 \cdot l_1} = -0.301A$$

$$I_2 := \frac{T_1 \cdot (N_1 \cdot V_{in} - V_{out} + 2 \cdot V_{out} \cdot d)}{2 \cdot N_1 \cdot l_1} = 15.006A$$

$$P_{out} := \frac{(1 - d) \cdot d \cdot T_{sw} \cdot V_{in} \cdot V_{out}}{2 \cdot l_1 \cdot N_1} = 3.636kW$$



Inductor rms current

$$I_P := \sqrt{\frac{I_1^2}{3} + \frac{I_2^2}{3} + I_1 \cdot I_2 \cdot \frac{1 - 2 \cdot \theta_1}{180^\circ}} = 8.593A$$

Sec. switches rms current

$$I_{SW} := \sqrt{\frac{1}{3} \cdot \left(\frac{I_3}{N_1}\right)^2 \cdot \frac{t_3}{T_{sw}} + \frac{1}{3} \cdot \left(\frac{I_1}{N_1}\right)^2 \cdot \frac{t_4}{T_{sw}} + \frac{1}{3} \cdot \left[\left(\frac{I_1}{N_1}\right)^2 + \left(\frac{I_2}{N_1}\right)^2 + \frac{I_1 \cdot I_2}{N_1^2}\right] \cdot \frac{t_5}{T_{sw}}} = 9.589A$$

Prim. switches rms current

$$I_{SW} := \sqrt{\frac{1}{3} \cdot I_3^2 \cdot \frac{t_3}{T_{sw}} + \frac{1}{3} \cdot I_1^2 \cdot \frac{t_4}{T_{sw}} + \frac{1}{3} \cdot (I_1^2 + I_2^2 + I_1 \cdot I_2) \cdot \frac{t_5}{T_{sw}}} = 5.993A$$

Output capacitor rms current

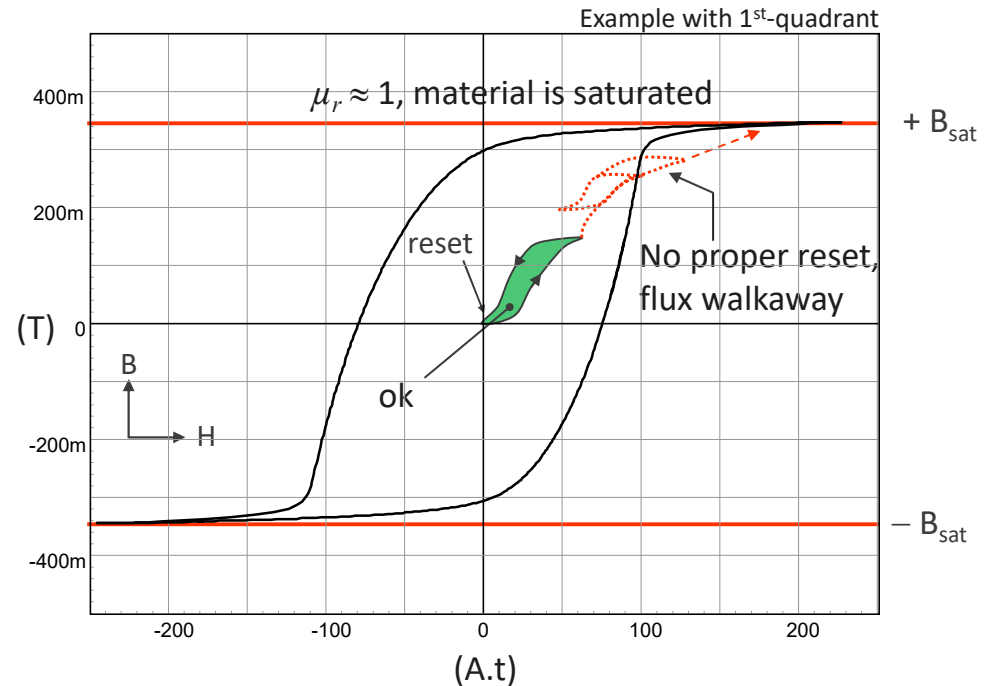
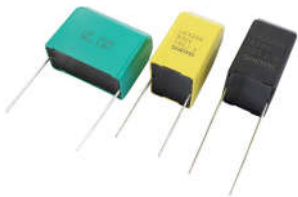
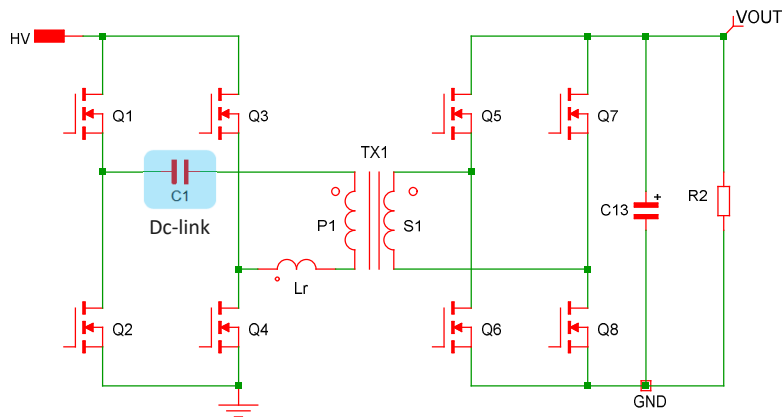
$$I_C := \sqrt{I_{outR}^2 - I_{out}^2} = 7.048A \quad 6.82 \text{ A rms}$$

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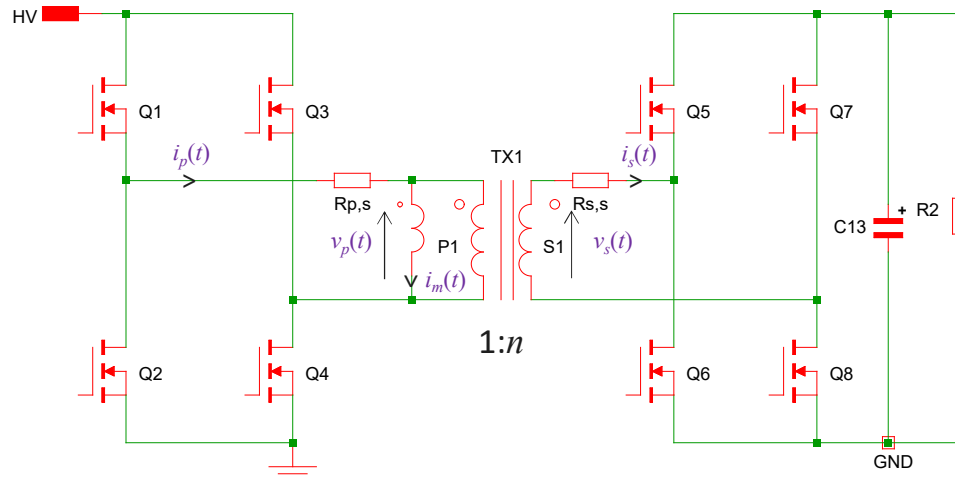
The Need to Demagnetize

- Core losses are linked to the magnetizing current and associated ΔB in the material
- Dc bias shifts the operating point and can cause saturation with catastrophic failure
- A dc-block capacitor is a solution, but it sees a large rms current and hampers cost



The Origin of the Drift

- Small variations in the control variables can affect the transformer volt-seconds:
- ✓ Semiconductor forward voltage drops move with temperature
- ✓ Insufficient pulse width modulator resolution can cause severe mismatches
- ✓ Gate driving signal delays affect the effective on- and off-time durations

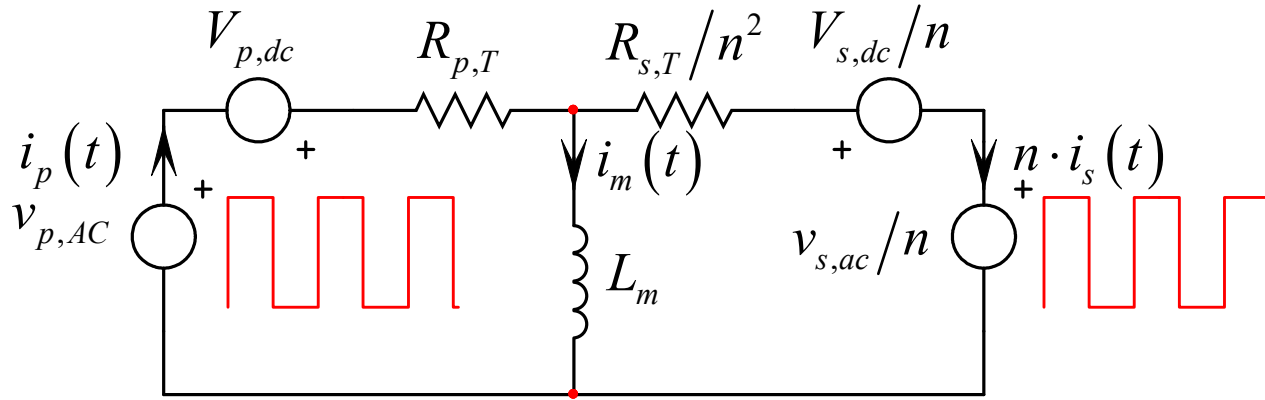


- The primary current i_p is made of the magnetizing current i_m plus the reflected output current:
- $$i_m(t) = i_p(t) - n \cdot i_s(t)$$
- It is possible to lump all ohmic drops into equivalent resistances in series with the primary and secondary:

$$I_{m,dc} = I_{p,dc} - n \cdot I_{s,dc} = \frac{V_{p,dc}}{R_{p,T}} - n \frac{V_{s,dc}}{R_{s,T}}$$

Modeling the Drift

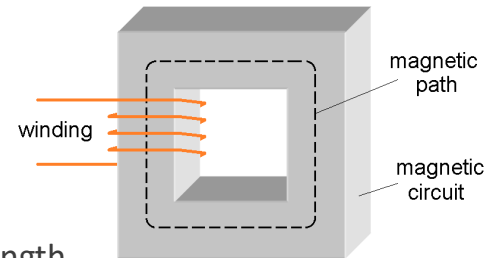
- The dc magnetic flux density depends on the winding and the core
- It is limited by the equivalent series resistances $R_{p,T}$ and $R_{s,T}$
- ✓ These resistances are extremely low for the best possible efficiency



$$H = \frac{NI}{l_m} \quad B = \mu_0 \mu_r H$$



$$B = \frac{N_p \cdot I_{m,dc}}{l_m} \mu_0 \mu_r$$



$$B_{dc} = \left(\frac{V_{p,dc}}{R_{p,T}} - n \frac{V_{s,dc}}{R_{s,T}} \right) \cdot \frac{N_p}{l_m} \cdot \mu_0 \mu_r$$

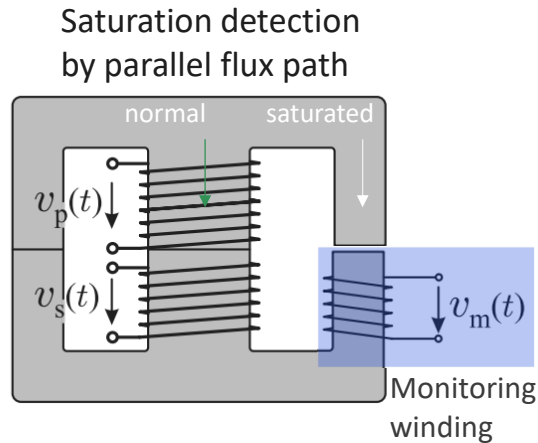
mean magnetic path length

Assessing Transformer Flux Imbalance

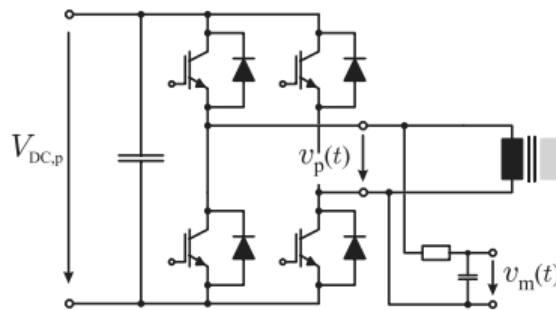
- The drift can be significant in a high-power converter:

$$R_{p,T} = 1.7 \text{ m}\Omega \quad F_{sw} = 20 \text{ kHz} \quad P_{out} = 166 \text{ kW} \quad F_{sw} = 20 \text{ kHz} \quad \mu_r \approx 1950$$

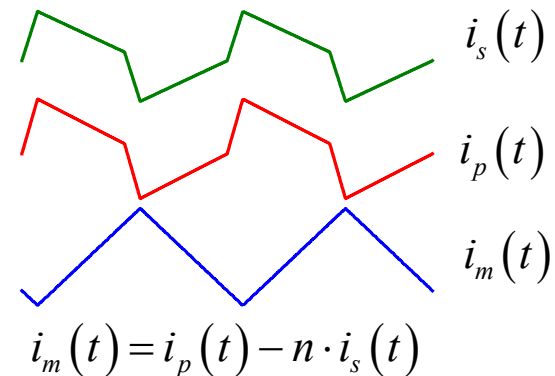
- Material is N87 with a μ_r of 1950 and the error in on- off-primary duration is 0.0125%
- This is a 2.5-ns timing error which leads to dc flux density component of $B_{dc} = 50 \text{ mT}$
- ❖ Risks of saturation, nonlinear magnetizing current and higher core losses under dc bias



Dynamic flux measurement

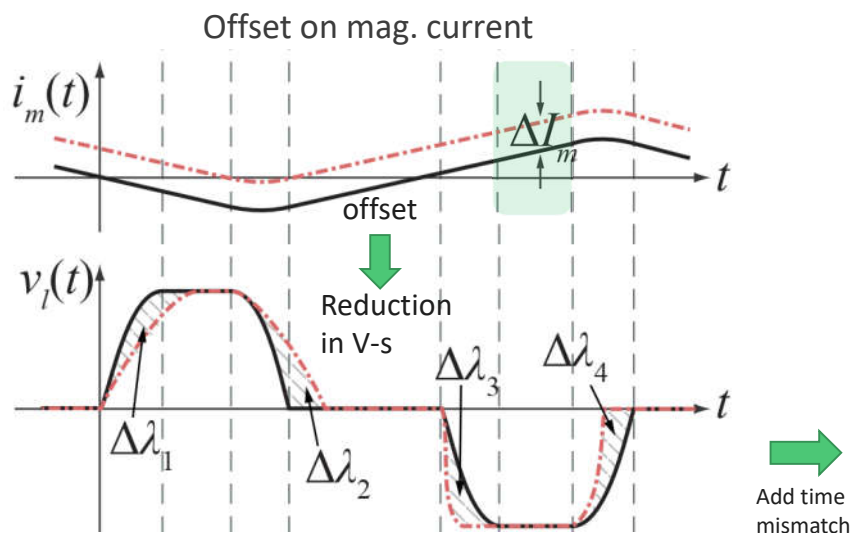


Magnetizing current reconstruction

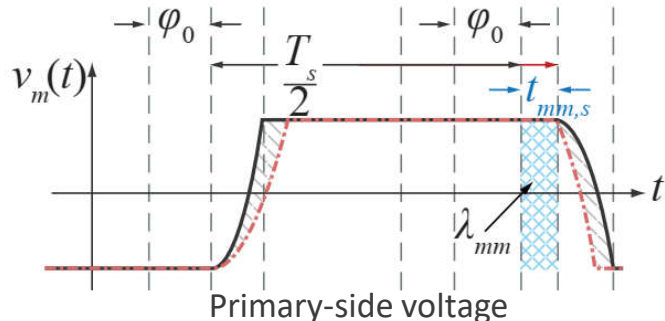


Fighting Transformer Flux Imbalance

- A series capacitor is possible with all the associated penalties (passive balancing)
- A gap is introduced to increase the saturation current, but it does not fix the problem
- Zero-Voltage Switching can partially compensate mismatch in V-s



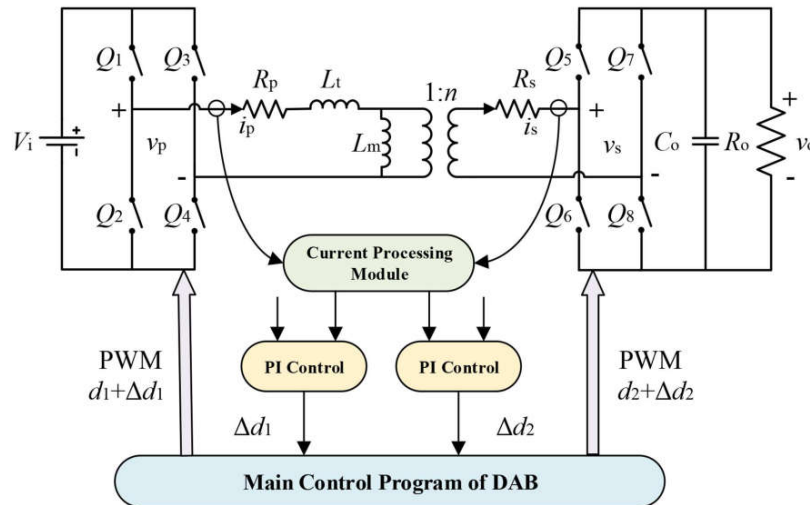
- ✓ The current offset speeds up the resonant transition and reduces flux linkage
- ✓ The time mismatch t_{mm} increases the V-s but the resulting dc offset speeds-up transitions which offers a counter measure



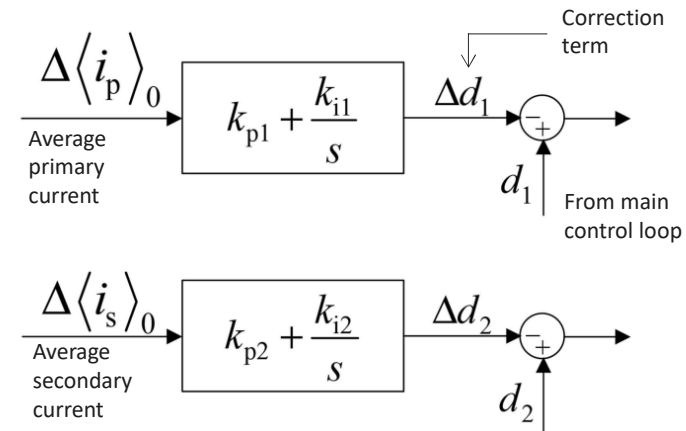
$$\Delta I = \frac{2V_g t_{mm,\varphi}}{2 \sum_{i=1}^2 \frac{\Delta\lambda_i}{\Delta I}}$$

Active Control

- Active flux control requires the monitoring of the primary- and secondary-side currents
- Two loops are implemented with two different processing paths
- One loop keeps a zeroed magnetizing current, a second zeroes the average prim. current
- Having i_m and i_p zeroed on average implies a zeroed average sec. side current



- A small PWM Δd modulation is added to the setpoint and keeps the dc offset to zero as a goal

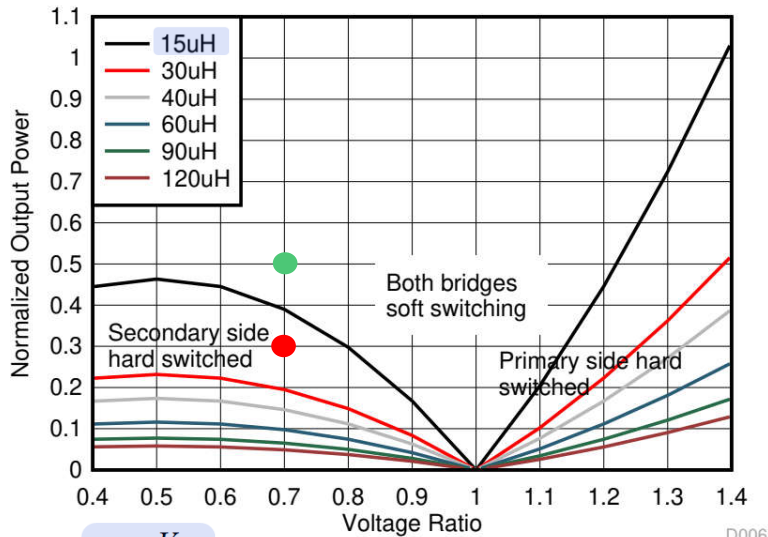


Agenda

- Phase-Shift Control
- Determining Inductor Currents
- Controlling the Power Flow
- Current Stress in the Converter
- Transformer Operating Point
- **Switching Losses**
- Small-Signal Response

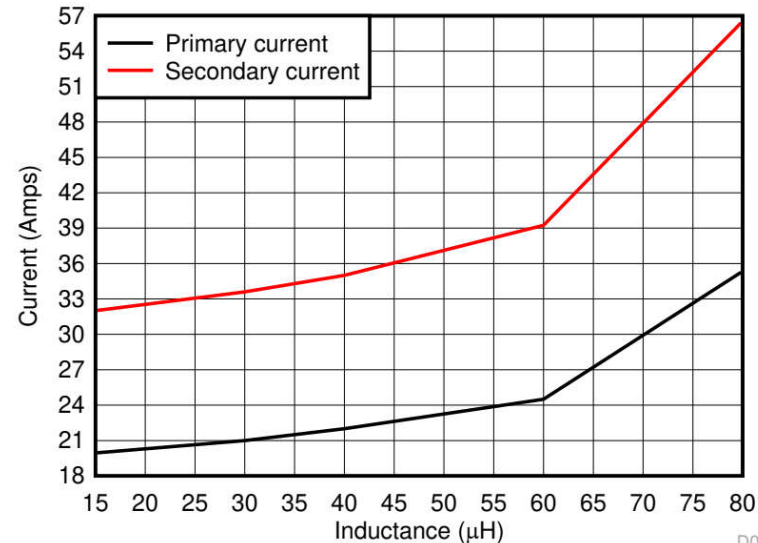
Effects of the Leakage Inductance

- The sweet spot for operating in soft switching is when M is unity
- The leakage inductance also determines the regions where soft switching is kept
- ✓ Having inductive current still circulating in light load ensures wide ZVS operation
- ❖ Too high an inductive current increases rms content and conduction losses



$$M = \frac{V_{out}}{NV_{in}}$$

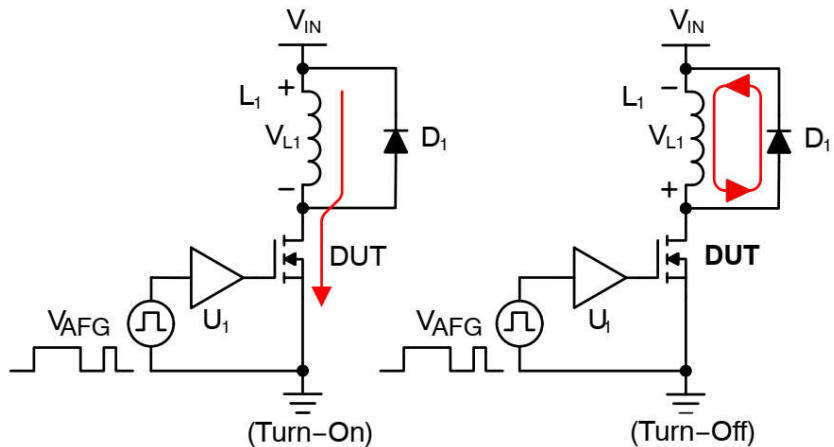
D006



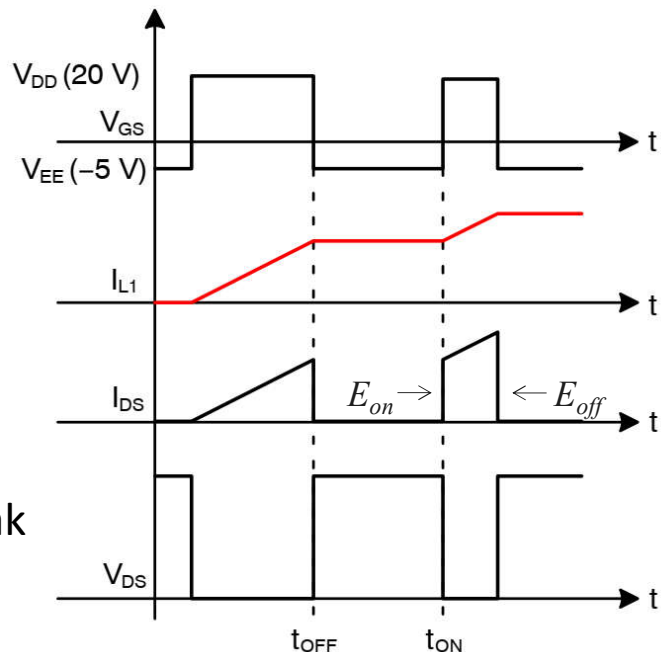
D004

Double-Pulse Test

- Transistors manufacturers provide curves graphing turn-on and -off losses
- These losses are evaluated using the double-pulse test
- ✓ Scaling to the operating parameters is necessary to evaluate the dissipated power

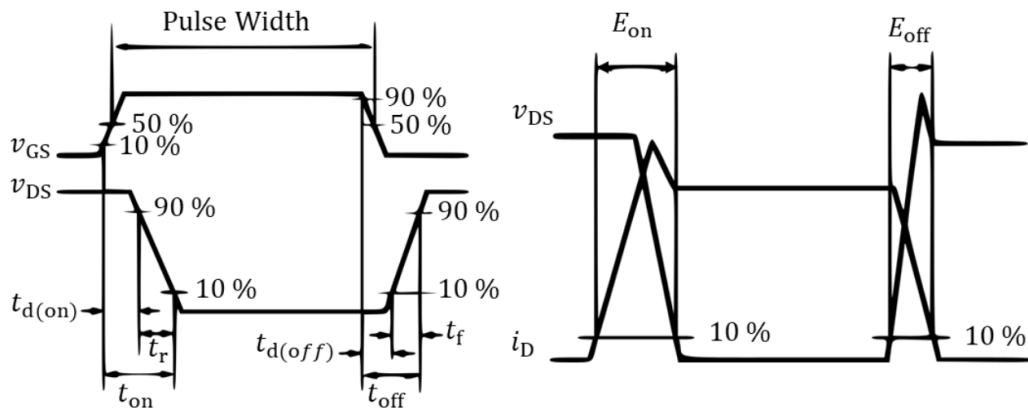


- A first pulse energizes the inductor at a given peak
- A second pulse ensures CCM operation



Evaluating Turn-On and Off Losses

- Transition losses are evaluated according to the IEC 60747-8 standard (MOSFETs)



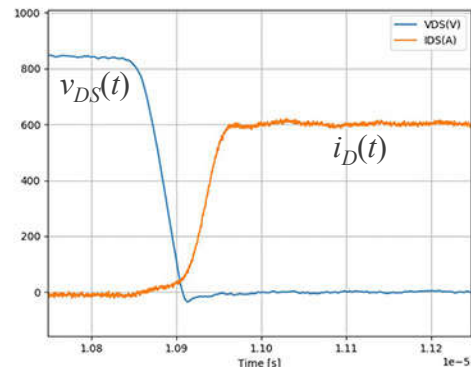
$$E_{on} = \int_{t_1}^{t_2} i_D(t) \cdot v_{DS}(t) \cdot dt$$

$$E_{off} = \int_{t_3}^{t_4} i_D(t) \cdot v_{DS}(t) \cdot dt$$

Typical values found in a data-sheet

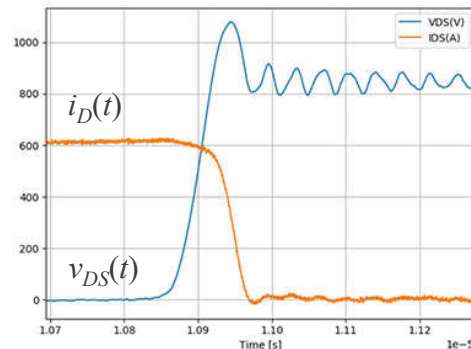
E_{ON}	Turn-On Switching Energy (Body Diode FWD)	246	μJ
E_{OFF}	Turn Off Switching Energy (Body Diode FWD)	99	

$V_{DS} = 600 \text{ V}$, $V_{GS} = -4 \text{ V}/15 \text{ V}$, $I_D = 35 \text{ A}$,
 $R_{G(\text{ext})} = 2.5 \Omega$, $L = 59 \mu\text{H}$, $T_J = 150^\circ\text{C}$



Turn-on losses

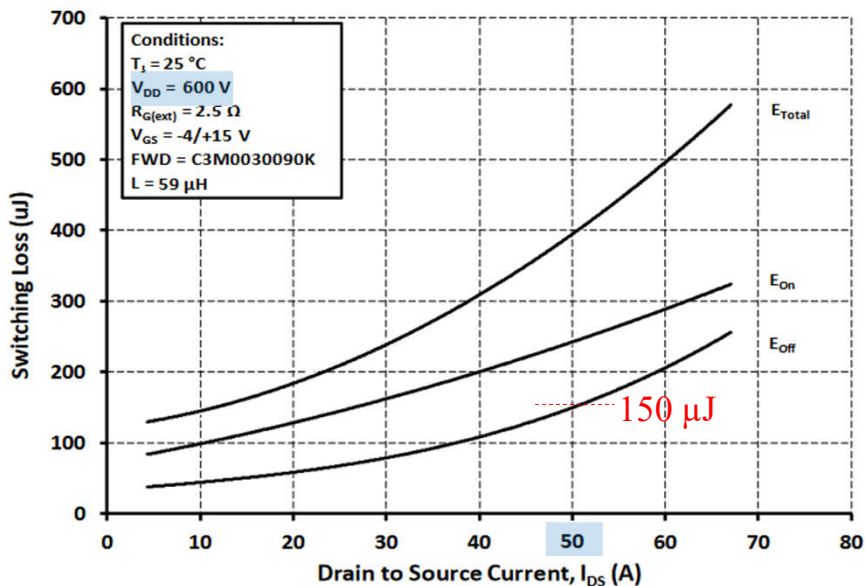
[Wolfspeed](#)
300-kW
Inverter



Turn-off losses

Scaling Losses in the SiC Transistors

- Transistors manufacturers provide curves plotting turn-on and -off losses
- These losses are evaluated using the double-pulse test in *ideal* conditions
- ✓ Scaling to the operating parameters is necessary to evaluate the dissipated power



[C3M0030090K](#)

Primary-side losses

$$P_{\text{off,prim}} = F_{sw} E_{\text{off}} \cdot k_2 \quad k_2 = \frac{I_{\text{prim}} V_{in}}{V_{DS} I_D}$$

Secondary-side losses

$$P_{\text{off,sec}} = F_{sw} E_{\text{off}} \cdot k_1 \quad k_1 = \frac{I_{\text{sec}} V_{out}}{V_{DS} I_D}$$

$$F_{sw} = 100\text{ kHz} \quad V_{out} = 500\text{ V}$$

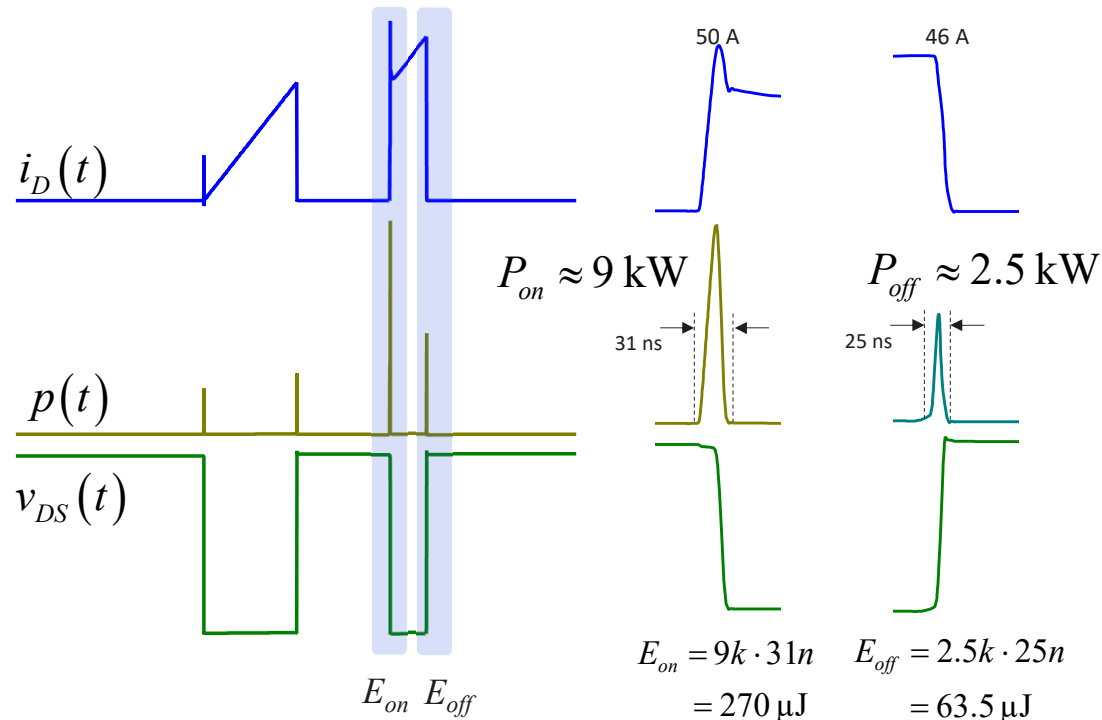
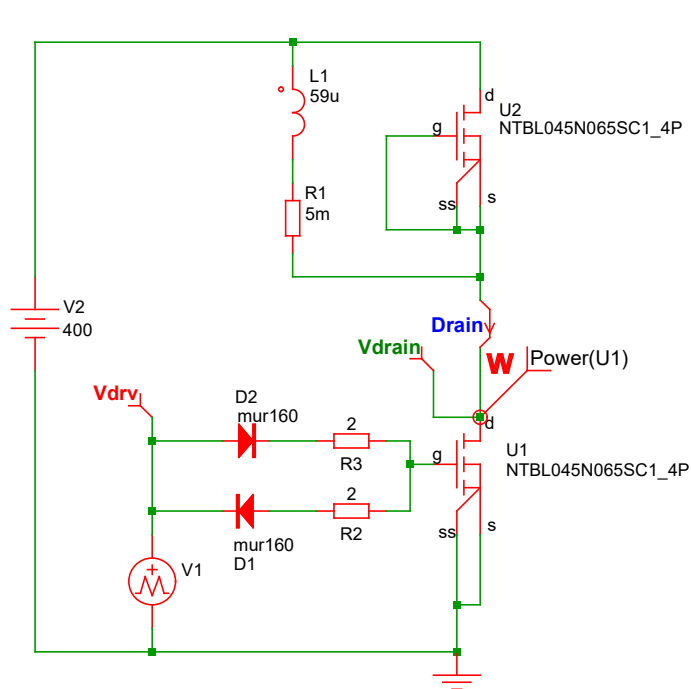
$$E_{\text{off}} = 150\ \mu\text{J} \quad I_{\text{sec}} = 35\text{ A}$$



$$P_{\text{off,sec}} = 100k \times 150u \times \frac{35 \times 500}{50 \times 600} = 10.5\text{ W}$$

SIMatrix[®] Double Pulse Simulation

- *onsemi* provides scalable SPICE models that can be imported into a simulator
- It is possible to measure switching losses in test conditions reflecting the application



Agenda

- Phase-Shift Control
- Determining Inductor Currents
- Controlling the Power Flow
- Current Stress in the Converter
- Transformer Operating Point
- Switching Losses
- Small-Signal Response

Small-Signal Model of the DAB – Output Sources

- A simple 1st-order model can easily be determined via an averaging process
- Express the output power and differentiate with respect to control variables d and V_{in}

Large-signal equation

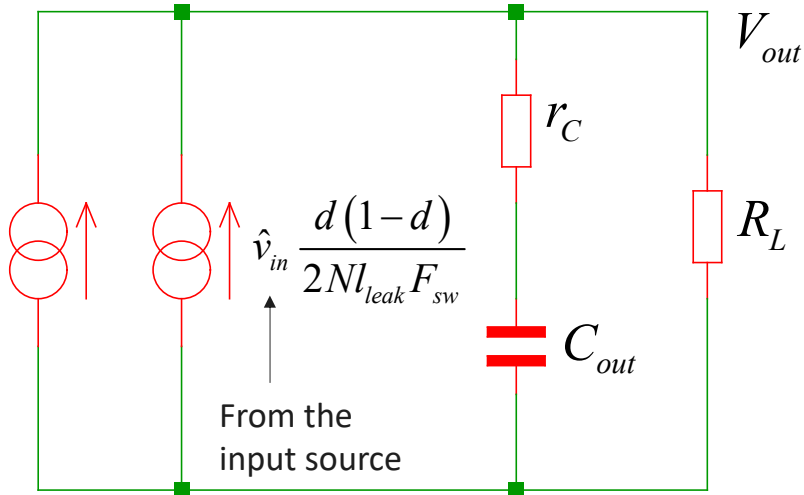
$$I_{out} = \frac{P_{out}}{V_{out}} = \frac{(1-d)dT_{sw}V_{in}}{2I_{leak}N}$$



$$\hat{i}_{out} = \frac{\partial I_{out}(d)}{\partial d} \hat{d} + \frac{\partial I_{out}(V_{in})}{\partial V_{in}} \hat{v}_{in}$$

$$\hat{d} \frac{V_{in}(1-2d)}{2Nl_{leak}F_{sw}}$$

From the modulator



- You obtain the control-to-output and input-to-output transfer functions

Small-Signal Model of the DAB – Input Sources

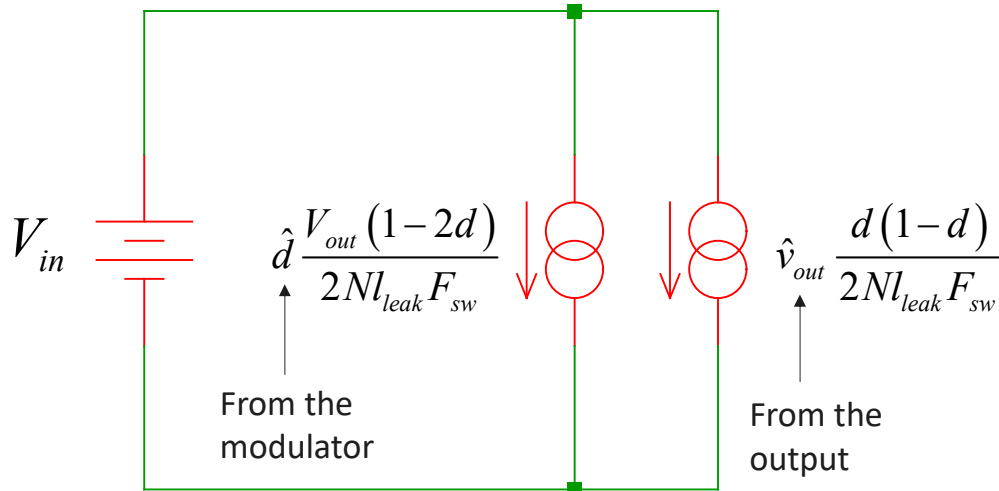
- Proceed with a similar process for the input side
- Express the input power and differentiate with respect to d and V_{out}

Large-signal equation ($\eta = 100\%$)

$$I_{in} = \frac{P_{in}}{V_{in}} = \frac{(1-d)dT_{sw}V_{out}}{2l_{leak}N}$$



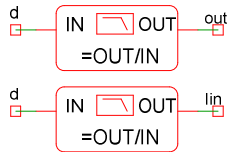
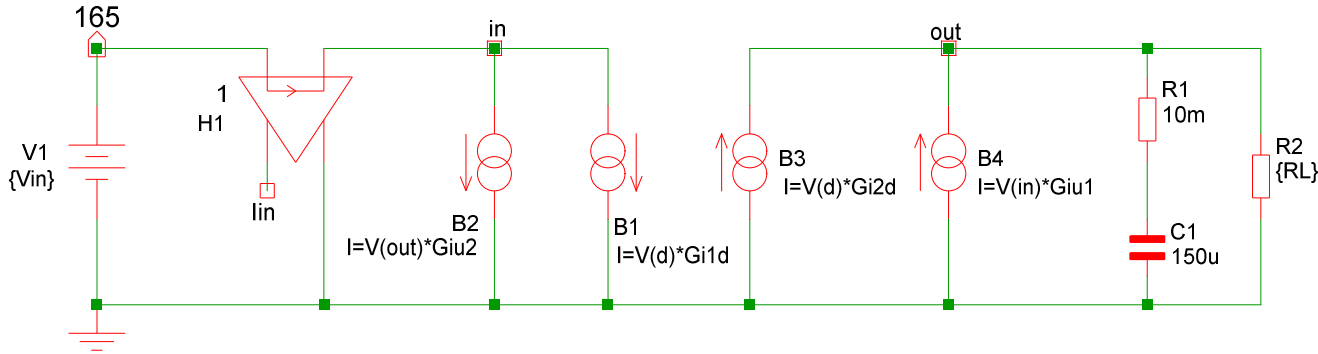
$$\hat{i}_{in} = \frac{\partial I_{in}(d)}{\partial d} \hat{d} + \frac{\partial I_{in}(V_{out})}{\partial V_{out}} \hat{v}_{out}$$



- It is easy to derive the small-signal open-loop input impedance of the DAB

Checking Responses with SIMetrix

- A SPICE model can be assembled with these four current sources
- It becomes easy to plot all needed transfer functions



```

Vout = 345
Vin = 165
Pout = 12k
RL = 9.91875
D = 63m
N = 2
Fs = 50k
Lr = 1.4u
Gi1d = 1.0768928571k
Giu2 = 210.825m
Gi2d = 515.035714286
Giu1 = 210.825m
H1.gain = 1
    
```

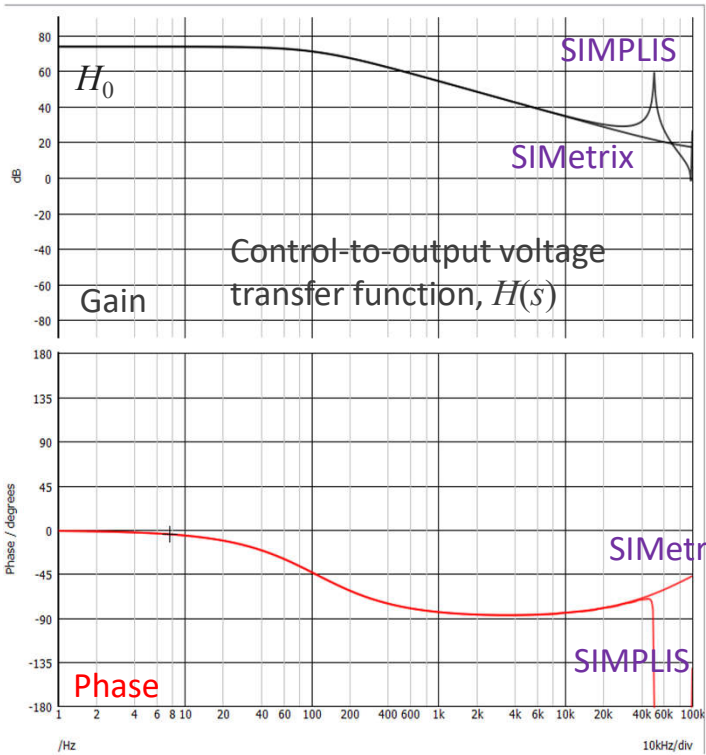


```

*
.PARAM Vout=345
.PARAM Vin=165
.PARAM Pout=12k
.PARAM RL={Vout^2/Pout}
*
.PARAM D=0.063
*
* DAB Components values
*
.PARAM N=2
.PARAM Fs=50k
.PARAM Lr=1.4u
*
.PARAM Gi1d={Vout*(1-2*D)/(2*N*Fs*Lr)}
.PARAM Giu2={D*(1-D)/(2*N*Fs*Lr)}
.PARAM Gi2d={Vin*(1-2*D)/(2*N*Fs*Lr)}
.PARAM Giu1={D*(1-D)/(2*N*Fs*Lr)}
*
{* *}
{* *}
{* *} Gi1d = {Gi1d}
{* *} Giu2 = {Giu2}
{* *} Gi2d = {Gi2d}
{* *} Giu1 = {Giu1}
{* *}
{* *}
*
    
```

SIMatrix and SIMPLIS Ac Responses

- The two simulators deliver identical responses for these transfer functions:
- ✓ Control-to-output voltage and control-to-input current

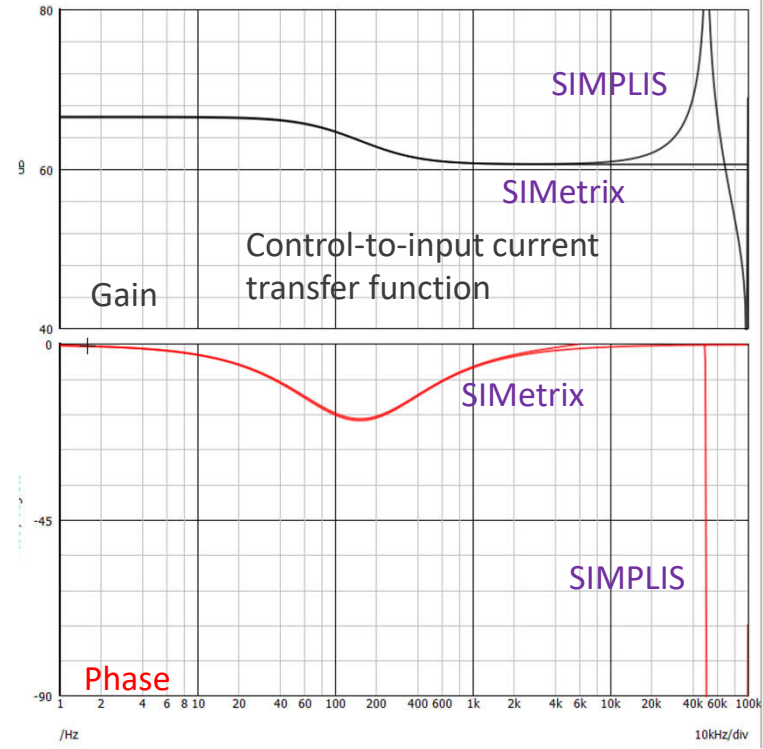


$$H(s) = H_0 \frac{1 + \frac{s}{\omega_z}}{1 + \frac{s}{\omega_p}}$$

$$H_0 = \frac{V_{out}}{V_p} \frac{(1-2D)}{(1-D)D}$$

$$\omega_z = \frac{1}{r_C C_{out}}$$

$$\omega_p = \frac{1}{C_{out} R_L}$$



Compensation of the Dual Active Bridge

Extracted from plant TF

```
.VAR Gfc=38 * magnitude at crossover *
.VAR PS=-83 * phase lag at crossover *
```

* Enter Design Goals Information Here *

```
.VAR fc=1k * targeted crossover *
.VAR PM=60 * choose phase margin at crossover *
```

* Enter the Values for Vout and Bridge Bias Current *

```
.VAR Vout=500
.VAR Ibias=1m
.VAR Vref=2.5
.VAR Rlower=Vref/Ibias
.VAR Rupper=(Vout-Vref)/Ibias
```

* Do not edit the below lines *

```
.VAR boost=PM-PS-90
.VAR G=10^(Gfc/20)
.VAR k=tan((boost/2+45)*pi/180)
.VAR fp=fc*k
.VAR fz=fc/k
.VAR C2=1/(2*pi*fc*G*k*Rupper)
.VAR C1=C2*(k^2-1)
.VAR R2=k/(C1*2*pi*fc)
```

* Choose op amp characteristics *

```
.GLOBALVAR AOL=90 * open-loop gain in dB *
.GLOBALVAR POLE=30 * low-frequency pole *
.GLOBALVAR VHIGH=5 * upper output level *
.GLOBALVAR VLOW=100m * lower output level *
```

* Do not edit these lines *

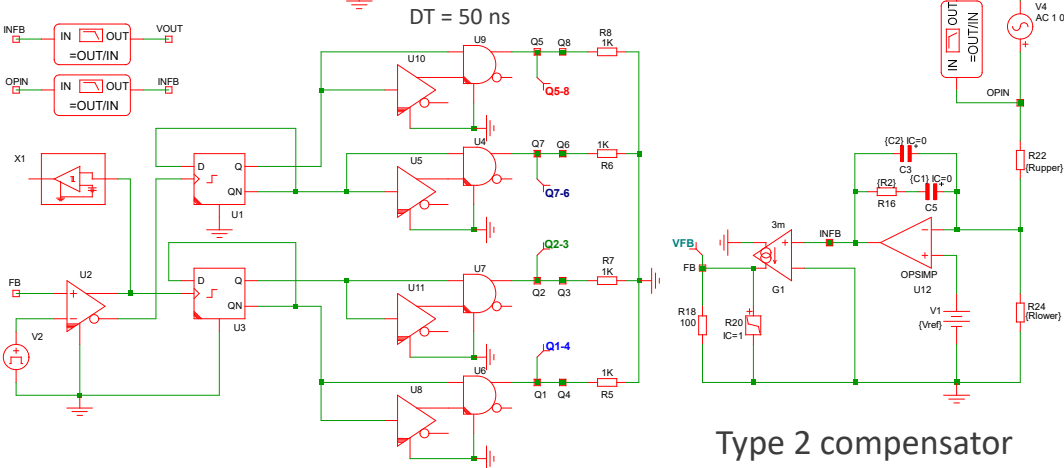
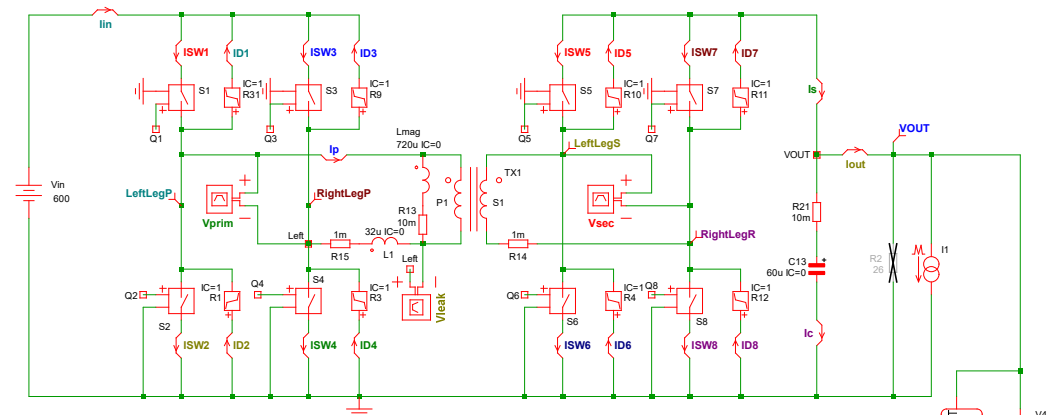
```
.GLOBALVAR gm=100u
.GLOBALVAR GAIN=(10^(AOL/20))
.GLOBALVAR COL=1/(6.28*(GAIN/100u)*POLE)
.GLOBALVAR ROL={GAIN/100u}
```

```
*
{ '*1 }
{ '*1 }
* Rupper = {Rupper}
{ '*1 } Rlower = {Rlower}
{ '*1 } k = {k}
{ '*1 } R2 = {R2}
{ '*1 } C2 = {C2}
{ '*1 } C1 = {C1}
{ '*1 } Boost = {boost}
{ '*1 } Fz = {Fz}
{ '*1 } Fp = {Fp}
{ '*1 } ROL = {ROL}
{ '*1 }
{ '*1 }
```



Automatically-calculated values

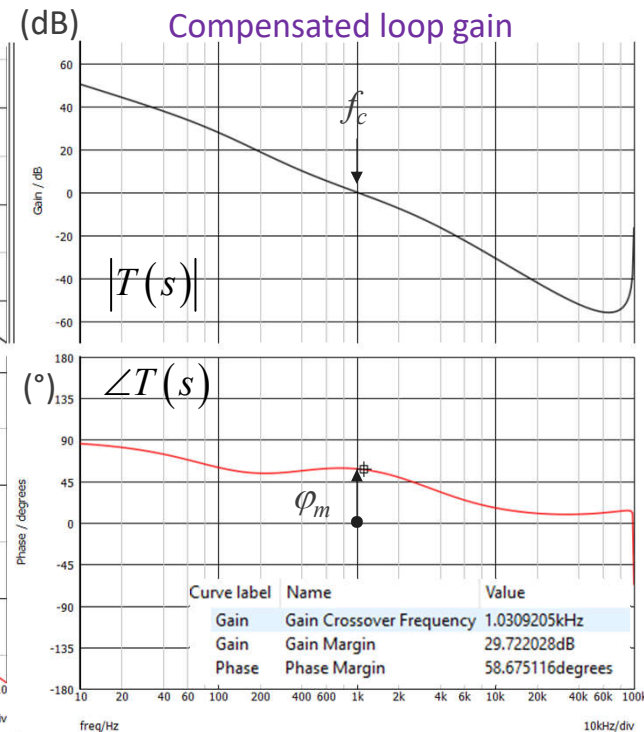
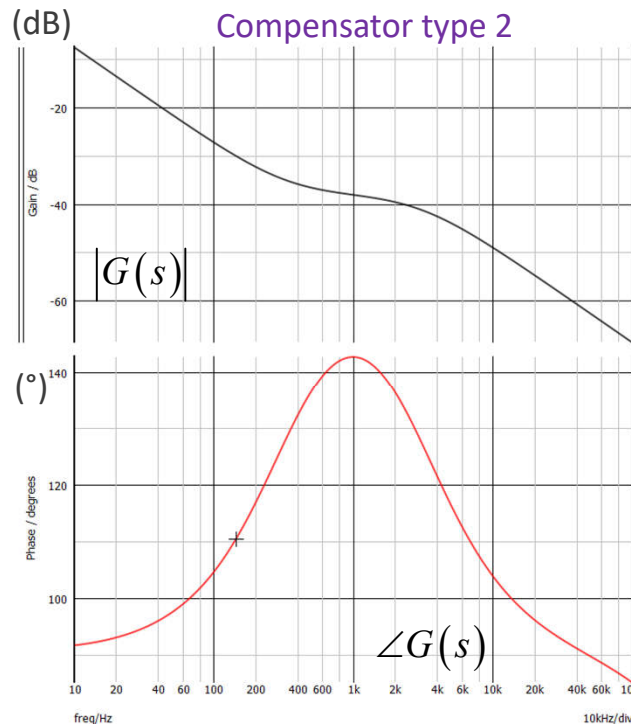
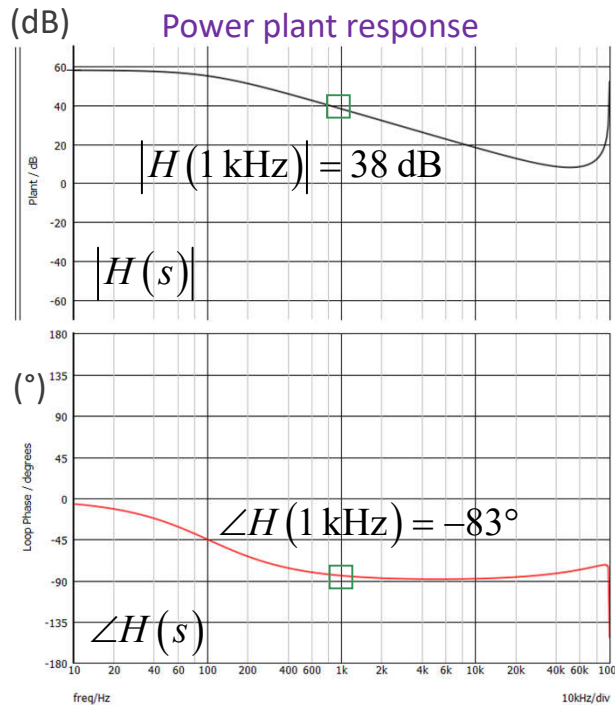
```
14 .tran 16m 11m
15 *
16 *
17 * Rupper = 497500
18 * Rlower = 2500
19 * k = 2.98868496274289
20 * R2 = 7052.73614201588
21 * C2 = 8.50250523667665e-09
22 * C1 = 6.74438934885475e-08
23 * Boost = 53]
24 * Fz = 334.595319502073
25 * Fp = 2988.68496274289
26 * ROL = 316227766.016838
27 *
28 *
```



Type 2 compensator

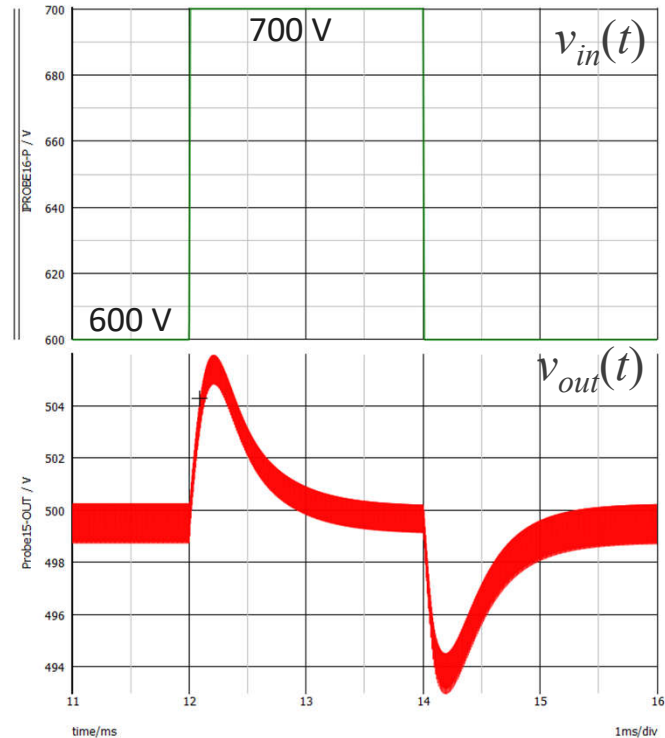
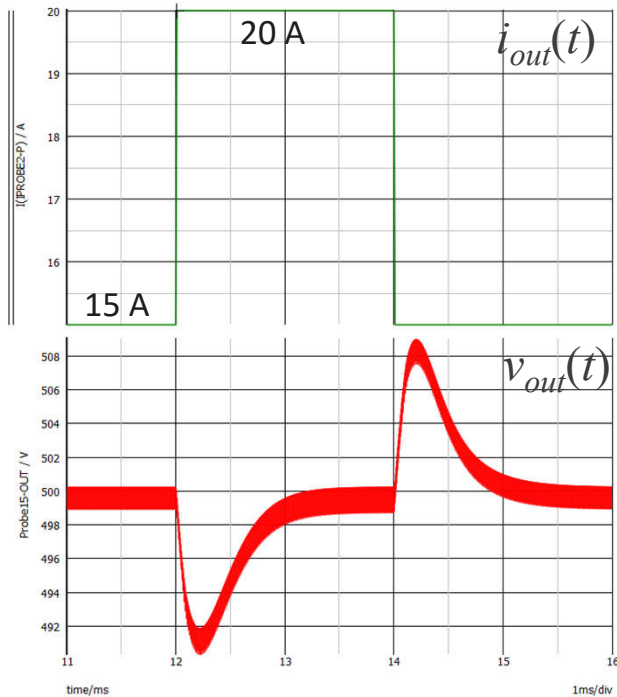
Control-to-Output Transfer Function

- Read the ac response magnitude and phase graphs and extract data at crossover
- Place a pole and a zero to boost the phase at crossover and meet phase margin goals



Step-Load Response of the DAB Converter

- Output power is stepped from 7.5 kW to 10 kW from a 600-V input source
- The input voltage is then stepped from 500 to 600 V with a 10-kW load



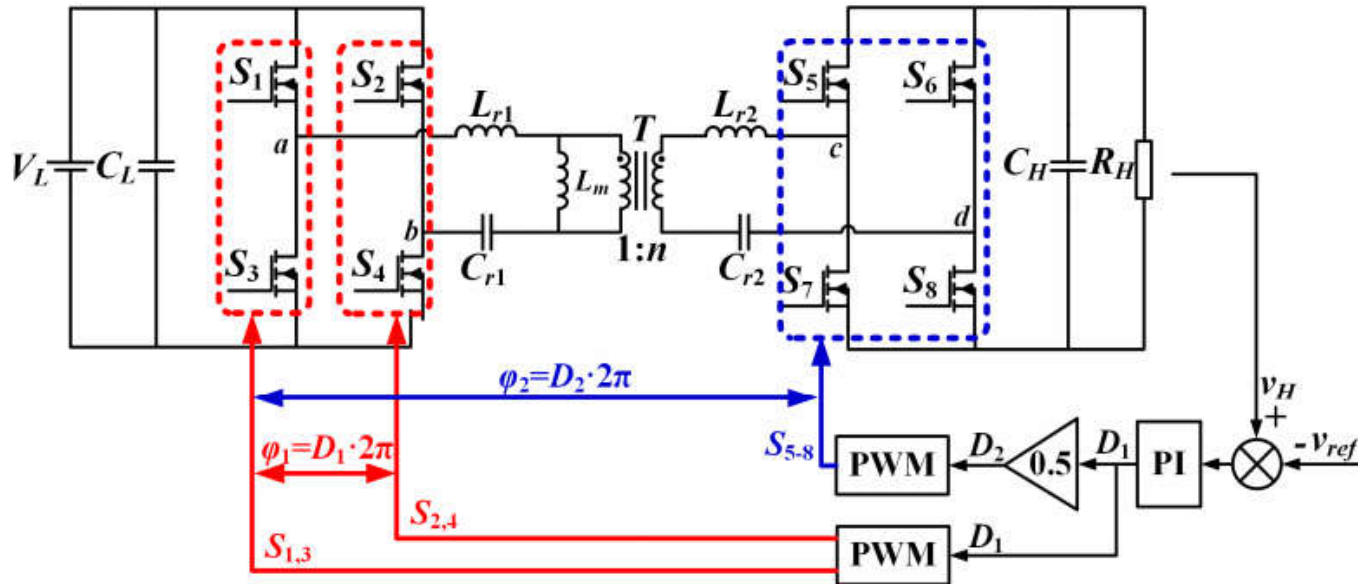
Conclusion

- A DAB converter implements two phase-shifted full bridges:
 - ✓ one in the primary and a second one for controlled rectification in the secondary
- A transformer scales the voltage between primary and secondary
- ✓ A series inductance – usually the leakage term – adjusts the maximum power transfer
- Power is controlled by driving the phase between the two bridges working at 50% duty ratio
- ✓ Depending on the phase polarity (lead or lag), power can flow either way: bidirectionality
- ✓ Different modulation schemes exist to minimize the circulating rms current
- It is also very important to check for the absence of dc shift in the operating transformer
- In voltage-mode control, the control-to-output transfer function is that of a 1st-order system

Backup slides

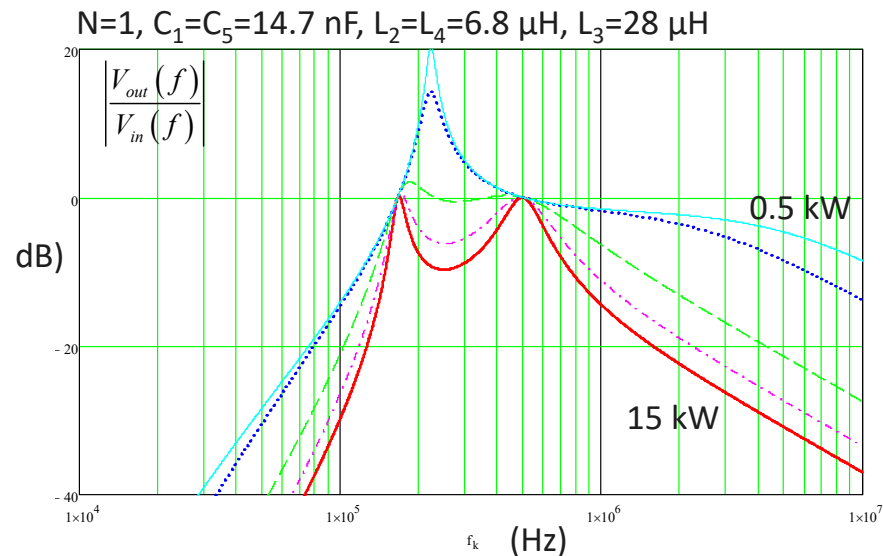
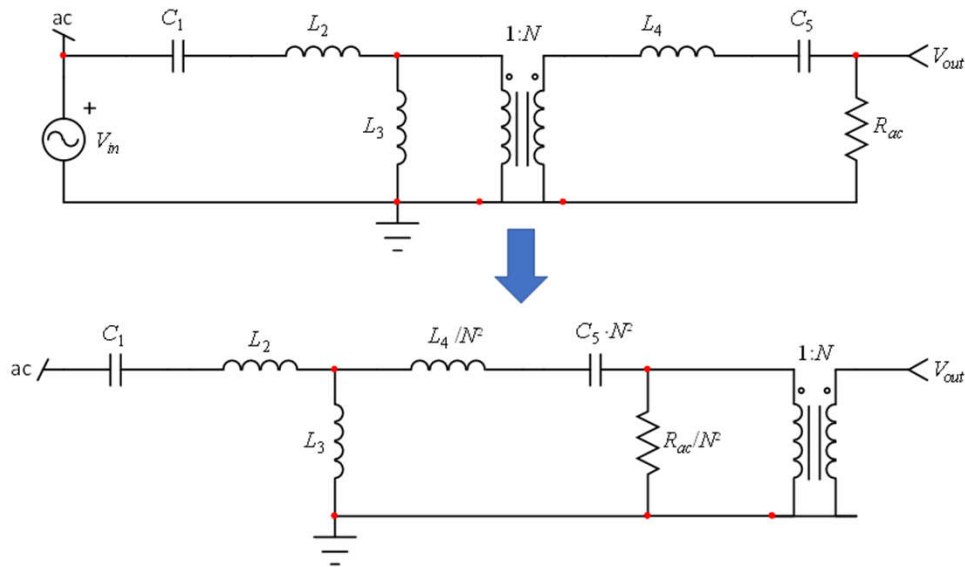
The CLLC Converter

- This is a resonant converter authorizing a bi-directional power flow
- Control can be by frequency modulation or phase shift
- Light-load regulation can be a problem with frequency modulation (flat gain curves)



Dc Transfer Characteristic of the CLLC

- The dc transfer characteristics link the input and output voltages
- Use first-harmonic approximation to derive an equivalent model

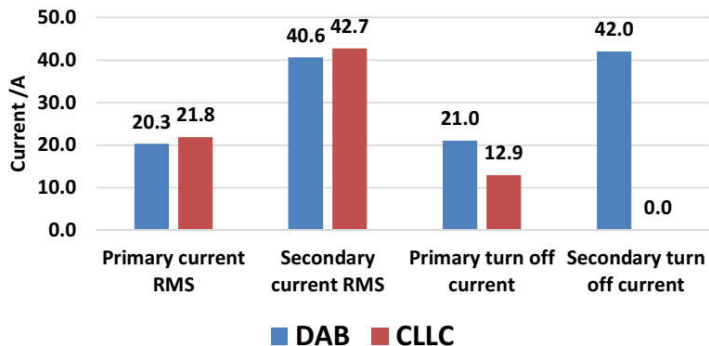


$$H(s) = N \frac{s^3 R_{ac} L_3 C_5 C_1}{1 + s R_{ac} C_5 + s^2 [C_1 (L_2 + L_3) + C_5 (L_3 + L_4)] + s^3 C_1 C_5 R_{ac} (L_2 + L_3) + s^4 C_1 C_5 (L_2 L_3 + L_2 L_4 + L_3 L_4)}$$

Comparison between DAB and CLLC

- Fixed-frequency operation
- ✓ 1 or several phase-shift/duty ratio control strategies
- ZVS depends on leakage inductance
- ✓ Increasing leakage for wider ZVS increases rms current
- Magnetizing inductance value is irrelevant
- Turn-off of switches occurs at maximum peak primary current, large E_{off}
- Equal gains in direct and reverse modes
- Variable frequency or phase-shift control
- ✓ Direct or indirect drive via charge control
- ZVS depends on magnetizing inductance
- ✓ ZVS is obtained in a large range
- ✓ Dead-time is selected accordingly
- ✓ Secondary-side switches operate in ZCS
- Turn-off of switches occurs at peak magnetizing current, smaller E_{off}
- Unequal gains in direct and reverse modes

Simulation Current Comparison



$V_{in} = 800$ V, $V_{out} = 400$ V, $F_{sw} = 500$ kHz, $P_{out} = 15$ kW, turns ratio 1:0.5, $I_{leak} = 2$ μ H, I_{leak} sec. = 0.5 μ H, L_{mag} LLC = 28 μ H

Device loss Comparison

